

from Monte Carlo variations

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ABSTRACT

The main s-process taking place in low-mass stars produces about half of the elements heavier than iron. It is therefore very important to determine the importance and impact of nuclear physics uncertainties on this process. We have performed extensive nuclear reaction network calculations using individual and temperature-dependent uncertainties for reactions involving elements heavier than iron, within a Monte Carlo framework. Using this technique, we determined the uncertainty in the main s-process abundance predictions due to nuclear uncertainties linked to weak interactions and neutron captures on elements heavier than iron. We also identified the key nuclear reactions dominating these uncertainties. We found that β -decay rate uncertainties affect only a few nuclides near s-process branchings, whereas most of the uncertainty in the final abundances is caused by uncertainties in neutron-capture rates, either directly producing or destroying the nuclide of interest. Combined total nuclear uncertainties due to reactions on heavy elements are in general small (less than 50 per cent). Three key reactions, nevertheless, stand out because they significantly affect the uncertainties of a large number of nuclides. These are 56 Fe(n, γ), 64 Ni(n, γ), and 138 Ba(n, γ). We discuss the prospect of reducing uncertainties in the key reactions identified in this study with future experiments.

Key words: nuclear reactions, nucleosynthesis, abundances – stars: abundances – stars: AGB and post-AGB – stars: evolution – stars: low-mass.

1 INTRODUCTION

Elements heavier than iron are mainly produced via neutron captures because the significant Coulomb barrier of these elements inhibits charged-particle captures. It is well established that the astrophysical origin of the majority of nuclides beyond Fe requires at least two neutron-capture processes (Burbidge et al. 1957; Cameron 1957), the so-called slow process (s-process) and rapid process (r-process): for the s-process the neutron-capture time-scale is generally longer than the β -decay time, whereas the opposite is true for the r-process.

* E-mail: gabriele.cescutti@inaf.it † BRIDGCE UK Network; www.bridgce.ac.uk In this work, we focus on the main component of the s-process, which takes place during the asymptotic giant branch (AGB) phase in low-mass stars, see e.g. Busso et al. (2001), Abia et al. (2002), Sneden, Cowan & Gallino (2008), and Zamora et al. (2009). The main neutron source for the s-process is the reaction 13 C(α ,n) 16 O (for a review of the main s-process, see Käppeler et al. 2011). This reaction is activated during the thermally pulsing AGB phase, taking place after central helium burning in low-mass stars. During this phase, energy production is dominated by the burning hydrogen shell and the helium shell flash events (thermal pulses, TPs), first described by Schwarzschild & Härm (1965). The TP starts when enough helium has been deposited by the hydrogen burning shell on top of the degenerate CO core and the helium shell becomes

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compressed and heated, see Herwig (2005). The helium shell ignites in an explosive way as the layers are degenerate, leading to a large energy flux and the extinction of the hydrogen burning shell. This large energy flux creates the pulse-driven convective zone (PDCZ) in the intershell, the area in between the core and the helium shell, which is expanding as a result of this energy flux. The expansion cools the region, allowing the helium shell to cool. The helium shell is now burning helium in a stable radiative manner until it runs out of fuel again. While the intershell region expands and cools, the convective envelope deepens. If the convective zone reaches sufficiently deep layers, it dredges up material enriched by the last PDCZ, a process called third dredge-up (TDU). Afterwards, the hydrogen shell re-ignites and the whole cycle repeats itself until the entire hydrogen-rich envelope has been lost by stellar winds. At the deepest point of penetration of the convective envelope, fresh protons are injected in the intershell, which is rich in ¹²C. Incomplete CNO cycling leads to a significant production of ¹³C in a narrow region below the convective envelope, which is often referred to as the ¹³C-pocket, see Gallino et al. (1998), Herwig (2005), Straniero, Gallino & Cristallo (2006), and the first description by Iben (1976) for more details. As this region later contracts as the TP cycle proceeds, it heats up and a large number of neutrons are released by the neutron source reaction ${}^{13}C(\alpha,n){}^{16}O$ in a radiative (nonconvective) layer (Straniero et al. 1995). A smaller contribution to the neutron flux comes from the $^{22}\mathrm{Ne}(\alpha,n)^{25}\mathrm{Mg}$ neutron source, which is activated in intermediate-mass stars at the bottom of the PDCZ (Abia et al. 2001) and, thus, releases neutrons in a convective environment. We will refer to the PDCZ phase as 'TP' phase in the rest of the paper.

Low-mass AGB stars are the sites for the main component of the s-process, i.e. elements between strontium and lead. The second component of the s-process (called weak component) takes place at the end of core helium burning and at the start of carbon (shell) burning in massive stars. Typically, it produces elements up to the Sr peak but depending on the metallicity and the mixing induced by rotation can also produce heavier nuclides (see Cescutti et al. 2016; Frischknecht et al. 2016; Prantzos et al. 2018). The neutron source for the weak s-process is 22 Ne(α ,n) 25 Mg.

There are several well-known uncertainties concerning the s-process production in low-mass stars. On the astrophysical side. the most important one is the general properties of the ¹³C-pocket and in particular its formation, see Cristallo et al. (2015), Battino et al. (2016), and Trippella et al. (2016) for a discussion and references. On the nuclear reaction side, Koloczek et al. (2016) (Ko16 hereinafter), recently reviewed the impact of current nuclear uncertainties considering both the ¹³C-pocket and TP conditions. As expected, they identify the neutron source reactions mentioned above as key reactions. They find that their uncertainties strongly affect the s-process production as do the competing reactions [see e.g. the discussion in Nishimura et al. 2014, for 22 Ne(α , γ) 26 Mg]. Neutron poison reactions, such as $^{14}N(n,p)$, $^{13}C(n,\gamma)$, $^{16}O(n,\gamma)$, and $^{22}\text{Ne}(n,\gamma)$ for the $^{13}\text{C-pocket}$ conditions, and $^{22}\text{Ne}(n,\gamma)$ and $^{25}\text{Mg}(n,\gamma)$ for the TP conditions, were also found to have a strong effect. The Ko16 study also identified a wide range of neutron captures as well as a few weak reactions on elements heavier than and including iron. When varying charged-particle reactions on light nuclides (as done in the Ko16 study), it may be necessary to conduct these sensitivity studies using full stellar evolution models. For instance, the adoption of a lower rate for the 13 C(α ,n) 16 O reaction could lead to the ingestion of some unburnt ¹³C in the PDCZ, with important consequences on the ongoing s-process nucleosynthesis (Cristallo et al. 2018). In this study, we only explore uncertainties in neutron captures and beta-decays on intermediate and heavy isotopes. We thus do not expect feedback effects from rate variations on the structure and the adopted post-processing approach is appropriate. Our approach to vary reaction rates is different from that of Ko16. We vary simultaneously all reaction rates in a Monte Carlo (MC) framework rather than one reaction at a time. Furthermore, we use temperature-dependent uncertainties based both on experimental and theoretical studies as we have already done for several other processes: the s-process in massive stars, γ -process in core collapse SNe, and γ -process in supernovae type Ia (Rauscher et al. 2016; Nishimura et al. 2017; Nishimura et al. 2018). We will compare our findings to those of Ko16 and comment further on similarities and differences of methods and results in the discussion section.

The paper is organized in the following way. In Section 2, we describe the astrophysical model used in this study as well as the MC framework PizBuin. In Section 3, we present the results of our sensitivity study and the list of key rates identified. We also discuss these key rates and the prospects to reduce their uncertainties with future experiments. In Section 4, we give our conclusions.

2 METHODS

In this section, we describe the main ingredients of our calculations: the thermodynamic trajectories used for the 13 C-pocket, the TP phase, and the MC PizBuin framework. The basic features of sprocess nucleosynthesis and the uncertainties of (n,γ) and weak rates determination are also summarized.

2.1 Astrophysical model

The complete evolution of low-mass stars is complex, especially during the TP-AGB phase. A full one-dimensional (1D) stellar model can require more than 100 000 time-steps and over one thousand spatial zones to be simulated completely from start to finish. It is thus not feasible to repeat such simulations 10 000 times as required by the MC procedure to complete a sensitivity study. We thus have to approximate the thermodynamic conditions inside the star with a trajectory following the key phase that we are studying. We start with the ¹³C-pocket case. The fact that this phase occurs under radiative conditions (rather than convective) makes it feasible to approximate it with a carefully selected single trajectory. This trajectory does not follow exactly what happens in real stars but, as shown below, provides the conditions that lead to an s-process production similar to that predicted using full stellar models.

The trajectory used in this work was extracted from a 3 ${\rm M}_{\odot}$, Z=0.014 (solar metallicity) stellar evolution model, calculated with MESA, revision number 6208 (Paxton et al. 2011). The trajectory was taken from the $^{13}{\rm C}$ -pocket following the 6th TP. The temperature and density profiles of the trajectory are shown in Fig. 1.

The trajectory starts after the ¹³C-pocket has formed. The formation of the ¹³C-pocket is the main uncertainty on the astrophysical side as mentioned above. The most advanced 3D models of stellar evolution are starting to resolve this phase in detail and Battino et al. (2016) have shown that using prescriptions in 1D stellar models guided by these 3D hydro simulations gives promising results. Most nucleosynthesis computations to date, however, typically take into account the ¹³C-pocket either by directly inserting a specific proton abundance profile below the convective envelope (e.g. Karakas & Lugaro 2016) or by assuming the mixing process that leads to it (Cristallo et al. 2011; Trippella et al. 2016). In this study, we artificially increase the ¹³C abundance, mimicking in this way the enhancement of ¹³C due to the injection of protons. We explored

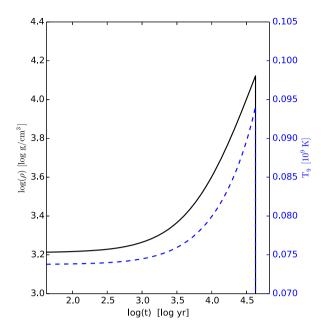


Figure 1. Time evolution of the temperature (GK) (blue dashed line) and density (solid black line) of the trajectory used for the ¹³C-pocket in this study.

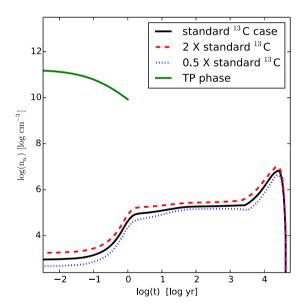


Figure 2. Time evolution of the neutron density (cm⁻³) for the three initial ¹³C abundances considered in the ¹³C-pocket and the TP phase.

variations in the initial content of 13 C that lead to an s-process production similar to the one predicted by full stellar models. Our tests revealed that an initial mass fraction of 13 C of $X_{^{13}\text{C}} = 1.95 \times 10^{-2}$ enables us to produce a typical s-process pattern with the above trajectory. We call our calculations using this value of 13 C our 'standard' case. To fully explore the range of conditions found in low-mass stars, we also used two additional initial 13 C abundances, one in which the standard initial abundance of 13 C is halved ('0.5 × 13 C' case), whereas in the other one it is doubled ('2 × 13 C' case). The variations in the neutron densities for the three cases are shown in Fig. 2. The initial composition for our calculations is given in Table 1 for nuclides for which we do not use the standard solar composition. Besides the change in 13 C explained above, the

Table 1. Initial composition for the nuclei that differ from the solar composition during the ¹³C-pocket.

Nuclei	Mass fraction	Nuclei	Mass fraction
¹ H	1.08×10^{-29}	¹⁶ O	4.32×10^{-2}
^{2}H	1.43×10^{-5}	¹⁷ O	2.80×10^{-6}
³ He	4.49×10^{-5}	¹⁸ O	4.83×10^{-8}
⁴ He	4.58×10^{-1}	¹⁹ F	1.79×10^{-9}
⁶ Li	6.44×10^{-10}	²⁰ Ne	1.23×10^{-3}
⁷ Li	9.15×10^{-9}	²¹ Ne	3.09×10^{-6}
⁹ Be	1.68×10^{-10}	²² Ne	3.12×10^{-2}
$^{10}{ m B}$	7.75×10^{-10}	²³ Na	3.10×10^{-5}
¹¹ B	3.43×10^{-9}	24 Mg	5.86×10^{-4}
¹² C	3.31×10^{-1}	²⁵ Mg	7.73×10^{-5}
¹³ C	1.95×10^{-2}	26 Mg	8.86×10^{-5}
¹⁴ N	5.11×10^{-3}	²⁷ Al	5.91×10^{-5}
¹⁵ N	9.02×10^{-8}	²⁸ Si	6.49×10^{-4}

Table 2. Initial composition for the light nuclei during the TP phase.

Nuclei	Mass fraction	Nuclei	Mass fraction
¹ H	5.35×10^{-23}	¹⁶ O	6.00×10^{-3}
^{2}H	1.37×10^{-5}	¹⁷ O	1.00×10^{-10}
³ He	4.29×10^{-5}	¹⁸ O	1.00×10^{-10}
⁴ He	7.91×10^{-1}	¹⁹ F	1.5×10^{-5}
⁶ Li	6.44×10^{-10}	²⁰ Ne	7.00×10^{-4}
⁷ Li	8.75×10^{-9}	²¹ Ne	1.00×10^{-5}
⁹ Be	1.68×10^{-10}	²² Ne	1.50×10^{-2}
$^{10}{ m B}$	7.41×10^{-10}	²³ Na	1.80×10^{-4}
^{11}B	3.28×10^{-9}	24 Mg	7.00×10^{-4}
¹² C	1.75×10^{-1}	²⁵ Mg	7.00×10^{-5}
¹³ C	1.50×10^{-7}	26 Mg	1.00×10^{-4}
¹⁴ N	5.00×10^{-3}	²⁷ Al	7.00×10^{-5}
^{15}N	5.00×10^{-6}	²⁸ Si	5.00×10^{-4}

other initial abundances for our calculations were extracted from the same stellar evolution model as the trajectory.

Besides the ¹³C-pocket, neutron captures also take place at the bottom of the TP-driven convective zone (PDCZ) as explained in the introduction. In low-mass AGB stars ($M < 4 M_{\odot}$), which dominate the overall s-process production given to the initial mass function), only a small production of neutron-rich isotopes is expected from the TP phase, such as ⁹⁶Zr (otherwise not produced during the radiative burning of the ¹³C-pocket). Given that the TP only contributes a short neutron burst and has a very small contribution to the overall s-process production, we approximated the TP conditions with a single-zone trajectory as in Ko16. The trajectory lasts for 1 yr, with a constant temperature of 0.245 GK and a constant density of 5 \times 10³ g cm⁻³. The initial abundances are summarized in Table 2 for light elements; for the other elements, the final abundances of the standard ¹³C-pocket were diluted by a factor of 20 to take into account the diluting effect of the PDCZ. The chosen trajectory, combined with the initial composition described above, is able to roughly reproduce typical isotopic compositions obtained during TP by more complex stellar evolution codes (Cristallo et al. 2015). The time evolution of the neutron density for the TP phase is also shown in Fig. 2.

2.1.1 Comparison to the Cristallo et al. (2011) yields

To validate our trajectory and initial composition combination, we compared the final abundances of our calculations at solar metallicity to the s-process pattern determined using full stellar models by Cristallo et al. (2011) (C11 hereinafter, but see also for details Straniero et al. 2006; Cristallo et al. 2009, 2007) for stars of 1.5, 2, and 3 M_{\odot} at solar metallicity. Our calculations used a single trajectory covering a single 13C-pocket whereas the C11 computed full stellar models. The s-process produced in the $^{13}\text{C-pocket}$ in their models is thus diluted into the convective envelope following the TDU. We thus used a dilution factor f to compare our final abundance to theirs. We set the dilution factor f to match the production of ^{88}Sr in our computations to the production in the $2\,M_{\odot}$ model of C11:

$$\frac{f^{88\text{Sr}}Y_{\text{out}}^{\text{traj}} + (1-f)^{88\text{Sr}}Y_{\text{ini}}^{\text{traj}}}{{}^{88\text{Sr}}Y_{\text{inij}}^{\text{traj}}} = \frac{{}^{88\text{Sr}}Y_{\text{out}}^{\text{C11}}}{{}^{88\text{Sr}}Y_{\text{ini}}^{\text{C11}}}$$
(1)

where 88 Sr $_{ini}^{traj}$ is the initial abundance of Sr in our trajectory, 88 Sr $_{out}^{traj}$ is the final abundance (same for the C11 production factors). Our final diluted abundances are compared to the C11 production factors in Figs 3, 4, 5, and 6.

The good overall agreement between our standard model and the C11 yields shows that our trajectory is adequate to determine the key nuclear reactions that strongly affect s-process predictions. Nevertheless, it is also clear that a single trajectory – as the one we adopt – is not able to reproduce the full range of conditions occurring in low-mass stars. We thus added to our investigations two other initial abundances for ¹³C, with the aim of covering a wider range of conditions of the s-process. It also allows us to determine the sensitivity of our results to the thermodynamic conditions and neutron flux in particular. Furthermore, since the main difference between models of main s-process production is the ratio between seed (given by the metallicity, mainly iron) and the neutrons (given by the ¹³C present at the start of the calculation) we are also investigating in some respect the metallicity dependence of this process. For the purpose of determining key rates, it is not necessary to match exactly the final results of Cristallo et al. (2011). More important is to investigate the full range of neutron fluxes and the activated branches. Figs 3, 4, 5, and 6 show that – excluding rare cases – the results we obtain with the three initial ¹³C contents cover the full range of results obtained by C11 and thus prove that our approach is suitable to determine the uncertain key rates for the s-process in low-mass stars. It is more difficult to apply a similar approach in the case of the TP phase. This is because the overall production during the TP is tiny compared to that occurring during the ¹³Cpocket. Therefore, there is no way to directly compare the output from this phase and the final theoretical results. We show in Fig. 7 the production factors of all the considered nuclei. There is significant production of only a few isotopes, and of these, most are not produced by our ¹³C trajectory (see Figs 3–6). These neutron-rich isotopes are in fact expected to mainly be produced during the TP phase in AGB stars (Gallino et al. 1998).

2.2 MC procedure

The thermodynamic trajectory described above was post-processed using the PizBuin code suite. This suite consists of a fast reaction network and a parallelized MC driver. We followed the same procedure as presented in detail in Rauscher et al. (2016). The nucleosynthesis calculation was repeated 10 000 times, with different rate variation factors each time, and the combined output was analysed subsequently. The simultaneous variation of rates is superior to a decoupled variation of individual rates as performed in the past and in Ko16 because neglecting a combined change in rates may

lead to an overemphasis of certain reactions and an overestimation of their impact on the total uncertainty (Rauscher et al. 2016; Rauscher et al. 2017).

In our method, we define key rates to be those dominating the uncertainty of a given final abundance. By this definition, reducing the uncertainty of a key rate will also considerably decrease the uncertainty in the final abundance of a given nuclide. The identification of key rates is obtained by examining the correlation between a change in a reaction rate and the change of an abundance. We used the Pearson product moment correlation coefficient to quantify these correlations. Positive values of the Pearson coefficients, r, indicate a positive correlation between rate change and abundance change, whereas negative values signify an inverse correlation, i.e. the abundance decreases when the rate is increased. The larger the absolute value of the Pearson coefficient, the stronger the correlation. As in Rauscher et al. (2016), Nishimura et al. (2017), and Nishimura et al. (2018), a level 1 key rate is identified by $r \ge 0.65$. Each astrophysical reaction rate involving elements from Fe to Bi was varied within its own uncertainty range. We used the same variation factor for forward and reverse rates as they are connected by detailed balance. The uncertainty range used is temperature dependent and constructed from a combination of the experimental uncertainty (if the rate has been measured) for target nuclei in their ground states and a theoretical uncertainty for predicted rates on nuclei in thermally excited states. Theory uncertainties were different depending on the reaction type and can be asymmetric. The reaction network consisted of 943 isotopes including all reactions relevant to the s-process, i.e. fusion reactions of lighter nuclei as well as (n, γ) reactions, electron captures, and β decays for heavier nuclei. The standard rate set and uncertainties used in this study are the same as in Rauscher et al. (2016) and Nishimura et al. (2017). Rates for neutron-, proton-, and α -induced reactions were a combination of theoretical values by Rauscher & Thielemann (2000) supplemented by experimental rates taken from Dillmann et al. (2006) and Cyburt et al. (2010); decays and electron captures were taken from a REACLIB file compiled by Freiburghaus & Rauscher (1999) and supplemented by rates from Takahashi & Yokoi (1987) and Goriely (1999) as provided by Aikawa et al. (2005) and Xu et al. (2013).

2.2.1 Nuclide selection for the key rate determination

Almost all the stable nuclides up to ²⁰⁹Bi have an s-process contribution. We might therefore present key rates for almost 250 isotopes. If an isotope, however, constitutes a negligible fraction of the total elemental abundance, improving its key reaction rates would not make a difference to the total production of an element. We thus had to establish a selection procedure for nuclides to be presented in our key rate determination. One possible selection method is to consider a threshold in the production factors. This method failed because it was not possible to determine a suitable threshold; either too few or too many nuclides were excluded and the resulting exclusions were rather random. Concerning the analysis of the ¹³Cpocket phase, we therefore decided to analyse only isotopes that contribute at least 10 per cent to the final total mass of the element. This selection method yields a list of 109 nuclides, most of which are listed in the tables below (note that only nuclides with a key rate are listed). In addition, we considered seven more nuclides ⁸⁶Sr, ⁸⁷Sr, ¹¹⁰Cd, ¹²³Te, ¹³⁴Ba, ¹⁴⁸Sm, and ¹⁷⁶Hf. Although their total production factor is below the 10 per cent threshold explained above, they are s-only nuclides and are thus worth investigating. Regarding the analysis of the TP phase, a similar procedure

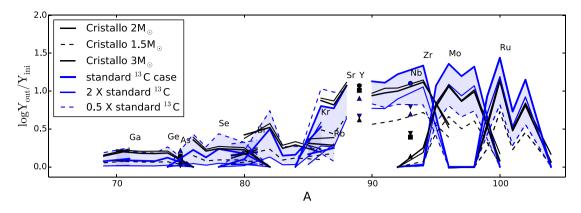


Figure 3. Production factors as a function of the atomic mass for elements from Ga to Ru during the 13 C-pocket. Comparison between the results obtained for a 1.5 (dashed black line – black triangle for monoisotopic elements), 2 (thick solid black line – black square), and 3 M $_{\odot}$ (thin solid black line – upside down black triangle) by C11 and the trajectory considered in this study with the three different initial abundances for 13 C: standard case (thick solid blue line – blue dot), half (dashed blue line – blue triangle), and double (thin solid blue line – upside down blue triangle) the standard case. The blue area highlights the range of s-process production obtained using the three cases for the initial 13 C abundance. Note that we applied a dilution factor, f, to our results to compare them to production factors of C11 (see equation 2.1.1).

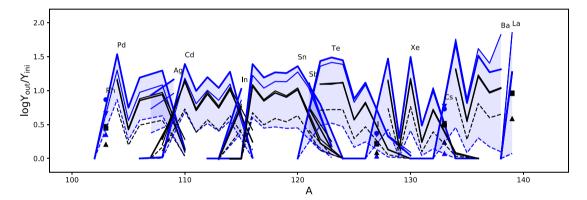


Figure 4. Same as Fig. 3 for elements from Rh to La.

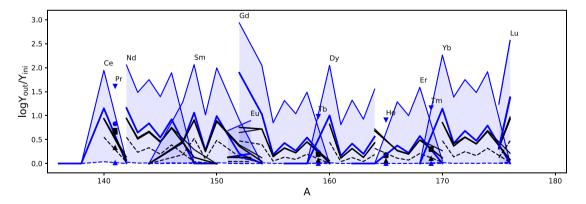


Figure 5. Same as Fig. 3 for elements from Ce to Lu.

fails to select all the isotopes that characterized this production; we therefore select all the isotopes not destroyed whose production is above 1 per cent of their production during the ¹³C-pocket phase. In this way, we exclude isotopes that have negligible production during the TP phase. To the isotopes selected in this way, we have added the s-only nuclides and the final list contains 58 nuclei (see Table 4).

3 RESULTS AND DISCUSSION

As explained above, we used the PizBuin code suite to determine the uncertainty in the final s-process abundances due to uncertainties of reactions involving heavy elements as well as the key reactions dominating these uncertainties. The total uncertainties of the final abundances are given in Table 3 for the ¹³C-pocket and in Table 4 for the TP phase and shown in Figs 8 and 9, respectively.

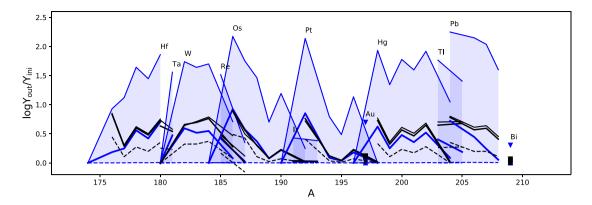


Figure 6. Same as Fig. 3 for elements from Hf to Bi.

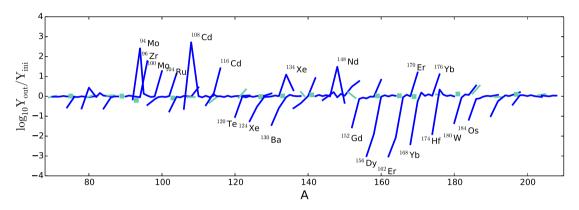


Figure 7. Production factors (final abundances divided by the initial abundances used for the TP trajectory) as a function of the atomic mass for elements from Ga to Pb during the TP phase. The blue lines connect elements with even atomic number, other elements are presented in cyan. Isotopes with a production factor greater than 10 or less than 0.1 are indicated.

3.1 Total uncertainties

As can be seen in Table 3 and Fig. 8, the overall uncertainties during the ¹³C-pocket are generally small. Indeed, most of them are smaller than 50 per cent. This is not too surprising since the relevant temperature range (~8 keV) is accessible to experimental measurements for many of the relevant rates, which are along the valley of stability, have already been measured experimentally. Furthermore, excited states generally have a weak contribution in this temperature range so the nuclear uncertainties are generally small to start with. There are nevertheless several nuclides, for which uncertainties are larger than a factor of 2. These are generally nuclides around branching points such as ⁸⁶Kr. We also notice a propagation effect for nuclides more massive than ¹³⁸Ba. This is due to the combined effect of uncertainties in neutron-capture rates above ¹³⁸Ba. For the TP case, we find somewhat larger uncertainties (see Table 4 and Fig. 9), in several cases greater than a factor of 2, and in four cases reaching a factor of 3. This is both due to the higher temperatures encountered, and the effect that at branching points there is a stronger sensitivity to the ratio between beta-decay rates and capture rates.

3.2 Key rates

As explained in Section 2.2, key rates are obtained by examining the correlation between a change in a reaction rate and the change of an abundance. The key reaction rates are listed in Table A1 for levels 1, 2, and 3 (for an explanation of key rate levels, see Section 3.2.1). Most of them are neutron-capture reactions either

directly producing or destroying the nuclide in question. This is not surprising because steady-flow equilibrium applies to most of the s-process path between the peaks. We nevertheless list all of them in the Appendix for completeness. Moreover, not all of the selected isotopes and key reactions appear at same level or with the same correlation, thus indicating the impact of specific reactions, or the impact of different degrees of constraint in experimental uncertainty on final abundances. Notable exceptions for the ¹³Cpocket are neutron captures on 56Fe, 64Ni, and 138Ba, which are level 2 key rates for many nuclides. We will come back to these three reactions in Section 3.4.1. There are also a few key weak reactions at branching points, ⁷⁹Se, ⁸⁵Kr, and ¹²⁸I. We will discuss the possibility of reducing the uncertainties of the key reactions linked to the most uncertain final abundances in Section 3.6. For the TP phase, there are two exceptions, the neutron-capture reactions 56,57 Fe(n, γ). While this may be surprising at first, 56,57 Fe act as 'poisons' in the TP phase. Indeed, they compete for neutrons with heavier nuclides and the neutron burst in the TP phase is too short for iron to act as a seed for the heavy elements produced during the TP.

3.2.1 Uncertainties for the different key reaction levels

As in our previous studies, we determined level 2 key reactions by using the standard rates for all previously identified (level 1) key reaction rates and performing another MC variation without varying those rates. This shows the effect when the level 1 key rates would have been determined. Level 2 key rates are then key

Table 3. Uncertainties in the final abundance of s-process nuclides from the MC calculation for the standard 13 C-pocket phase. The column labelled 'Level' indicates the level of the first key reaction found. The remaining columns show uncertainty factors for variations Up and Down, the values of which are $Y(95 \text{ per cent})/Y_{\text{peak}}$ and $Y(5 \text{ per cent})/Y_{\text{peak}}$, respectively. They enclose a 90 per cent probability interval, as shown in Fig. 8.

Nuclide	Level	Up	Down	Nuclide	Level	Up	Down
⁶⁹ Ga	1	1.13	0.896	¹³⁸ Ba	2	1.08	0.941
⁷¹ Ga	1	1.24	0.918	¹³⁹ La	1	1.34	0.922
⁷⁰ Ge	1	1.18	0.888	¹⁴⁰ Ce	2	1.12	0.877
⁷² Ge	1	3.23	0.944	¹⁴¹ Pr	2	1.09	0.854
⁷⁴ Ge	1	1.51	0.966	¹⁴² Nd	3	1.17	0.886
75 As	1	1.14	0.936	¹⁴⁴ Nd	_	1.14	0.860
⁷⁶ Se	1	1.17	0.939	¹⁴⁶ Nd	3	1.17	0.880
⁷⁸ Se	1	1.98	0.971	147 Sm	3	1.14	0.858
⁸⁰ Se	1	1.29	0.939	¹⁴⁸ Sm	3	1.19	0.889
$^{79}\mathrm{Br}$	1	2.79	0.962	150 Sm	3	1.17	0.878
⁸¹ Br	1	1.08	0.942	¹⁵¹ Eu	1	1.23	0.810
80 Kr	1	2.57	0.782	¹⁵³ Eu	-	1.14	0.842
82 Kr	1	1.25	0.940	152 Gd	3	1.18	0.768
⁸⁴ Kr	1	1.52	0.970	154 Gd	3	1.15	0.854
⁸⁶ Kr	1	1.78	0.472	156 Gd	3	1.15	0.852
⁸⁵ Rb	1	1.07	0.943	158 Gd	_	1.15	0.848
⁸⁷ Rb	1	1.94	0.514	¹⁵⁹ Tb	1	1.37	0.833
⁸⁶ Sr	1	1.17	0.945	¹⁶⁰ Dy	-	1.20	0.878
⁸⁷ Sr	1	1.15	0.957	162 Dy	-	1.17	0.855
⁸⁸ Sr	1	1.06	0.950	¹⁶⁴ Dy	3	1.20	0.861
⁸⁹ Y	1	1.10	0.926	¹⁶⁵ Ho	1	1.29	0.844
90 Zr	1	1.12	0.907	¹⁶⁶ Er	1	1.40	0.818
92 Zr	1	1.21	0.932	¹⁶⁷ Er	1	1.39	0.846
⁹⁴ Zr	1	1.13	0.923	¹⁶⁸ Er	1	1.57	0.826
⁹³ Nb	1	1.46	0.945	$^{169}\mathrm{Tm}$	1	1.76	0.806
⁹⁵ Mo	1	1.13	0.927	¹⁷⁰ Yb	_	1.21	0.873
⁹⁶ Mo	1	1.32	0.967	¹⁷² Yb	_	1.17	0.836
⁹⁷ Mo	1	1.12	0.910	¹⁷⁴ Yb	_	1.19	0.847
⁹⁸ Mo	1	1.26	0.927	¹⁷⁵ Lu	3	1.21	0.871
⁹⁹ Ru	1	1.20	0.943	¹⁷⁶ Lu	3	1.19	0.848
¹⁰⁰ Ru	1	1.19	0.908	¹⁷⁶ Hf	3	1.27	0.833
¹⁰² Ru	1	1.13	0.926	¹⁷⁸ Hf	-	1.22	0.866
¹⁰³ Rh	1	1.28	0.939	¹⁸⁰ Hf	_	1.19	0.841
¹⁰⁴ Pd	1	1.46	0.968	¹⁸¹ Ta	1	1.52	0.788
¹⁰⁶ Pd	1	1.42	0.943	¹⁸² W	_	1.20	0.837
¹⁰⁸ Pd	1	1.37	0.918	¹⁸³ W	3	1.20	0.800
¹⁰⁷ Ag	1	1.11	0.936	¹⁸⁴ W	-	1.23	0.859
109 Ag	1	1.08	0.914	¹⁸⁵ Re	-	1.19	0.820
¹¹⁰ Cd	2	1.05	0.939	¹⁸⁶ Os	_	1.25	0.852
¹¹² Cd	2	1.06	0.952	¹⁸⁷ Os	1	1.72	0.820
¹¹⁴ Cd	2	1.06	0.953	¹⁸⁸ Os	3	1.22	0.825
¹¹⁵ In	1	1.39	0.912	¹⁹⁰ Os ¹⁹¹ Ir	_	1.22	0.827
¹¹⁶ Sn ¹¹⁸ Sn	1	1.05	0.938	¹⁹¹ Ir ¹⁹³ Ir	_	1.20	0.820
¹²⁰ Sn	2	1.07	0.948	¹⁹³ Ir ¹⁹² Pt	3	1.31	0.815
¹²¹ Sb	2	1.06	0.953	¹⁹⁴ Pt	1	2.31	0.871
¹²¹ Sb ¹²² Te	1	1.19	0.954	¹⁹⁶ Pt	1	2.91	0.850
¹²³ Te	-	1.06	0.957	¹⁹⁷ Au	3	1.32	0.795
¹²⁴ Te	- 2	1.04	0.945	¹⁹⁸ Hg	-	1.24	0.838
¹²⁶ Te	3	1.06	0.955	²⁰⁰ Hg	2	1.31	0.782
¹²⁷ I	1 1	1.07	0.950	²⁰² Hg	1	1.36 1.34	0.774
¹²⁸ Xe	1	1.16 1.04	0.945	²⁰³ Tl	3		0.858
130 Xe	2	1.04	0.908 0.958	²⁰⁵ Tl	1	1.30 2.40	0.779
¹³² Xe	1	1.33	0.958	²⁰⁴ Pb	I -	1.27	0.772 0.797
¹³³ Cs	1	1.13	0.937	²⁰⁶ Pb	_	1.30	0.763
¹³⁴ Ba	1	1.13	0.949	²⁰⁷ Pb	_	1.43	0.763
¹³⁶ Ba	1	1.12	0.953	²⁰⁸ Pb	_	1.43	0.792
¹³⁷ Ba	1	1.12	0.954	²⁰⁹ Ві	3	1.39	0.746
Dа	1	1.09	0.930	DI	3	1.30	0.740

Table 4. Uncertainties in the final abundance of s-process nuclides from the MC calculation for the TP phase. The column labelled 'Level' indicates the level of the first key reaction found. The remaining columns show uncertainty factors for variations Up and Down, the values of which are $Y(95 \, \text{per cent})/Y_{\text{peak}}$ and $Y(5 \, \text{per cent})/Y_{\text{peak}}$, respectively. They enclose a 90 per cent probability interval, as shown in Fig. 9.

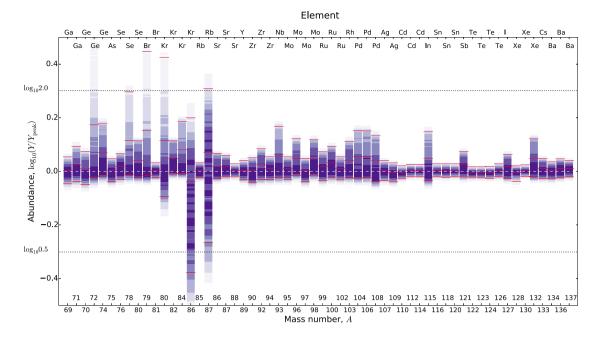
Nuclide	Level	Up	Down	Nuclide	Level	Up	Down
⁷⁰ Ge	1	1.04	0.946	¹³⁴ Ba	2	1.08	0.923
⁷⁶ Se	1	1.06	0.901	¹³⁶ Ba	1	1.03	0.988
⁸² Se	1	1.14	0.941	¹³⁸ La	1	2.56	0.919
80 Kr	1	1.11	0.789	¹⁴² Ce	1	3.42	0.619
⁸⁶ Sr	1	1.04	0.977	¹⁴² Nd	_	1.01	0.974
87Sr	1	1.05	0.960	¹⁴⁸ Nd	1	2.09	0.442
⁹⁶ Zr	1	3.73	0.469	148 Sm	2	1.10	0.862
⁹⁴ Mo	1	1.21	0.879	¹⁵⁰ Sm	1	1.11	0.956
⁹⁶ Mo	1	1.08	0.900	¹⁵² Sm	1	1.10	0.918
¹⁰⁰ Mo	1	1.73	0.466	¹⁵⁴ Sm	_	3.40	0.602
¹⁰⁰ Ru	1	1.11	0.912	^{152}Gd	1	1.41	0.263
¹⁰⁴ Ru	1	1.81	0.456	^{154}Gd	1	1.16	0.886
¹⁰⁴ Pd	1	1.31	0.956	160 Gd	1	2.14	0.500
¹¹⁰ Pd	1	1.39	0.388	$^{160}{ m Dy}$	1	1.29	0.884
¹⁰⁸ Cd	_	1.11	0.926	¹⁷⁰ Er	1	3.52	0.627
¹¹⁰ Cd	1	1.06	0.927	¹⁷⁰ Yb	1	1.94	0.727
¹¹⁶ Cd	1	1.39	0.256	¹⁷⁶ Yb	1	1.34	0.414
¹¹⁴ Sn	1	1.04	0.928	¹⁷⁶ Lu	1	1.12	0.867
¹¹⁵ Sn	1	1.05	0.923	$^{186}\mathrm{W}$	1	2.14	0.878
¹¹⁶ Sn	1	1.02	0.970	¹⁸⁷ Re	3	1.85	0.843
¹²⁴ Sn	1	1.07	0.783	¹⁸⁶ Os	1	1.20	0.674
¹²² Te	1	1.04	0.944	¹⁸⁷ Os	1	2.13	0.762
¹²³ Te	2	1.06	0.932	¹⁹² Os	1	1.28	0.680
¹²⁴ Te	1	1.01	0.973	¹⁹² Pt	1	1.92	0.686
130Te	1	1.40	0.927	¹⁹⁵ Pt	1	2.96	0.841
¹²⁸ Xe	1	1.04	0.883	¹⁹⁸ Pt	1	1.39	0.448
130 Xe	1	1.02	0.961	¹⁹⁸ Hg	1	1.13	0.890
¹³⁴ Xe	1	2.38	0.639	²⁰⁴ Pb	1	1.04	0.951
¹³⁶ Xe	1	2.06	0.835	²⁰⁹ Bi	1	1.02	0.996

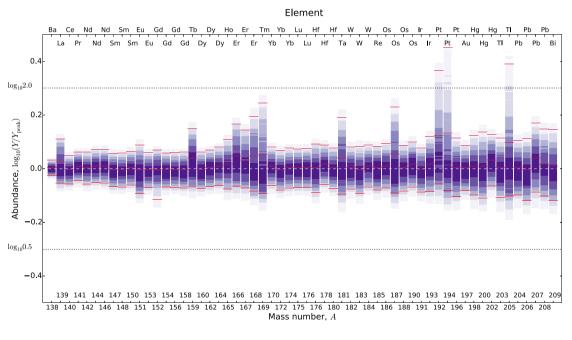
to the remaining uncertainties. Similarly, level 3 key rates were determined by exempting level 1 *and* level 2 key rates from the MC variation. It has to be emphasized that level 2 and level 3 key reactions are only important *provided that level 1 and level 2 rates, respectively, have been constrained.*

Figs 10 and 11 show the total uncertainties obtained for levels 2 and 3, respectively. We see that already at level 2, uncertainties are tiny for nuclides lighter than ¹³⁸Ba. Exceptions are a few isotopes at branching points (⁸⁰Kr, ⁸⁶Kr, and ⁸⁷Rb). The propagation effect for nuclides more massive than ¹³⁸Ba remains. The total uncertainty has already significantly decreased compared to level 1 so limited improvements can be made by future measurements of the level 2 rates. The level 3 uncertainties shown in Fig. 11 show that all key rates were identified at level 1 or 2 and that the uncertainties are negligible once these have been determined. The same is true for the TP phase.

3.3 Dependence of uncertainties and key rates on astrophysical conditions

We used a single-zone trajectory to mimic the astrophysical conditions taking place in the TP-AGB phase of low-mass stars in our MC calculations. A single-zone trajectory cannot capture the full conditions found in stars. As explained in Section 1, conditions vary in stars and there are still major uncertainties in the modelling of the TP-AGB phase and in particular concerning the formation





0.10 0.25 0.40 0.55 0.70 0.85 1.00 Frequency, $F/F_{\rm peak}(Y)$

Figure 8. Total production uncertainties in the final s-process abundances obtained with the trajectory described in the previous section for the ¹³C-pocket with the standard initial abundance. The colour shading denotes the probabilistic frequency and the 90 per cent probability intervals up and down are marked for each nuclide with the red lines. The final abundances are normalized by the final abundance at the peak of the distribution. Horizontal dotted lines indicate a factor of 2 uncertainties.

of the ^{13}C -pocket. Nevertheless, as our comparison to the yields of C11 in Section 2.1.1 shows, using an initial ^{13}C abundance divided ('0.5 \times ^{13}C ' case) and multiplied ('2 \times ^{13}C ' case) by a factor of 2 compared to the standard case samples the variations in the s-process production in stars of different masses. It also samples different neutron-to-seed ratios and thus to some extent the metallicity dependence of our results. More generally, it allows us to

determine the sensitivity of our results to the astrophysical conditions found in the ^{13}C -pocket. Figs 3, 4, 5, and 6 show that in the '0.5 \times ^{13}C ' case, the production stops around ^{138}Ba and therefore that this case underestimates the neutron flux needed to produce the main s-process. This leads to a stronger production for elements between iron and strontium. In the '2 \times ^{13}C ' case, the production is very strong all the way up to lead with overproduction factors much

Element

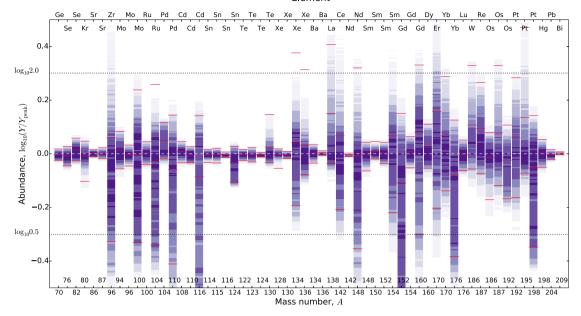


Figure 9. Total production uncertainties in the final s-process abundances obtained with the trajectory described in the previous section for the TP phase. The colour shading denotes the probabilistic frequency and the 90 per cent probability intervals up and down are marked for each nuclide with the red lines. The final abundances are normalized by the final abundance at the peak of the distribution. Horizontal dotted lines indicate a factor of 2 uncertainties.

larger than those of C11. This means that the neutron flux in this case is very strong and the elements between iron and strontium are depleted. We thus do not consider the two additional cases as representative cases for the main s-process. This is why we do not list the total uncertainties for these two cases in tables. Rather we use them to test the robustness of the key rates list against variations that are larger than the variations expected to occur in real stars.

The total uncertainties for the two additional cases are shown in Figs 12 and 13. Comparing these figures to Fig. 8 for the standard case, we see that the same nuclides have the largest uncertainties. We also see that uncertainties are generally small (less than 50 per cent) for most nuclides in the three cases. The main difference between the three cases is the extent of the propagation effects. Since the flow stops around barium for the '0.5 \times 13 C' case, the propagation effect is strongest in this case for elements around and above barium. In the '2 \times 13 C' case, propagation effects are very small because the production easily reaches lead.

We list the key rates for the three cases in Tables A1, A2, and A3 in the Appendix. Comparing Table A2 to Table A1, we see that all but one key rates for the '0.5 \times ¹³C' case were already key rates for the standard case. The exception is ²⁰⁹Bi(n, γ)²¹⁰Bi, which is not important in this particular case because there is no production beyond barium. Comparing Table A3 to Table A1, we see again that most key rates for the '2 \times ¹³C' case were already key rates for the standard case. The very strong flux in the '2 \times ¹³C' case leads to a production, which follows a slightly more neutron-rich path and thus to a few more key rates that were not present in the standard case. The strong overlap in the key reaction lists between the standard case and the other two cases representing a very weak and very strong neutron flux shows that our reference key reaction list is a representative of the full range of astrophysical conditions found in the ¹³C-pocket.

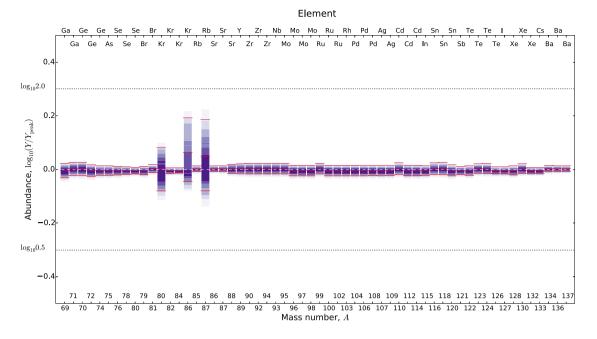
3.4 Comparison to past sensitivity studies

The key differences between the approach used in this study and past studies are explained in Rauscher et al. (2017) and Rauscher et al. (2016). We summarize them here:

- (i) Instead of varying rates one-by-one, all rates involving heavy elements in the network are varied simultaneously in an MC framework.
- (ii) Key reactions are identified by inspection of correlations in the simultaneous variation of all rates instead of relying on the sensitivity of an abundance to the individual variation of a single rate
- (iii) Each rate is assigned an individual uncertainty which is temperature dependent and which is sampled by a different MC variation factor for each rate. Uncertainties do not have to be symmetric.
- (iv) The bespoke rate uncertainties are derived and are based on both experimental data for the ground-state contributions when available and a theoretical uncertainty for the excited-states contributions.

Varying rates one-by-one may result in an incorrect assessment of total uncertainties as well as the importance of the selected rates. This is due to the fact that the combined action of several reactions can cover or enhance uncertainties in each single rate. We rather define a key reaction as a reaction dominating the uncertainty of the final abundance of a given nuclide. This means that this abundance uncertainty will be considerably reduced when better constraining the corresponding key reaction. Key reactions are specific to a nuclide and it is possible that no key reaction can be found for a given nuclide when many reactions are contributing to its abundance.

As explained in the Introduction, Koloczek et al. (2016) (Ko16) recently reviewed the impact on the main s-process of current nuclear uncertainties considering both the ¹³C-pocket and TP conditions. Ko16 varied reaction rates one-by-one so it is interesting to compare our results to theirs. Note that this study focused on inter-



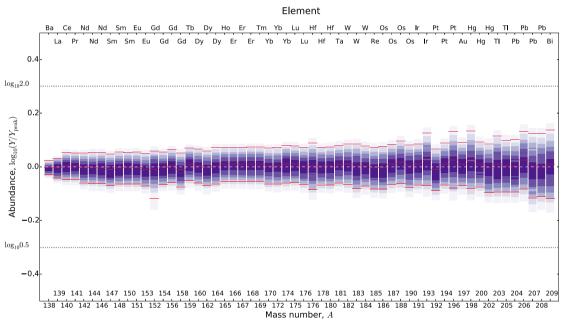
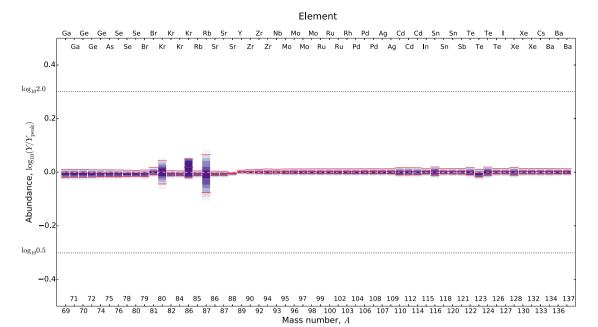


Figure 10. Same as Fig. 8 except that all the level 1 key reactions are now fixed to show the improvements that determining all level 1 rates would make.

 $0.10 \ 0.25 \ 0.40 \ 0.55 \ 0.70 \ 0.85 \ 1.00$ Frequency, $F/F_{
m peak}(Y)$

mediate and heavy elements and therefore this is the atomic mass range that we will compare. The uncertainties for rates involving light elements are generally well established and we refer the reader to the Ko16 and Käppeler et al. (2011) studies (and references therein) concerning nuclear uncertainties linked to light elements (e.g. neutron sources and neutron poisons). Ko16 provide a list of the strongest globally affecting reactions during both the TP (their Table A) and the ¹³C-pocket (their Table B), which is very valuable information. Since rates were varied individually, however, it is not

clear whether or not the rates in question dominate the uncertainties for all the nuclides affected by that reaction. Re-measuring the rates listed in tables A and B of Ko16 may thus not reduce the uncertainties in predicted production of all the nuclides affected. Our definition of key rates gives exactly this information since a rate is only key if it dominates the uncertainty of a given nuclide. Our study shows that in many cases, the key rates dominating the nuclear uncertainties are the neutron captures either directly producing or destroying the nuclide in question. Nevertheless, all the



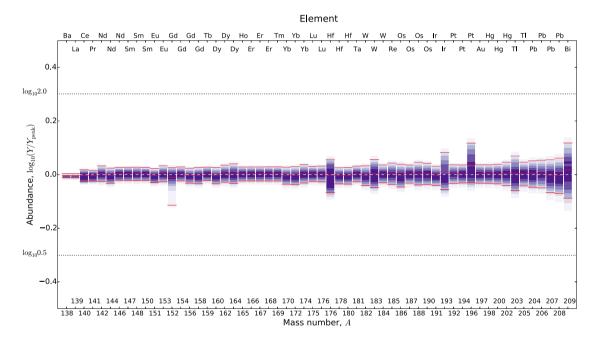
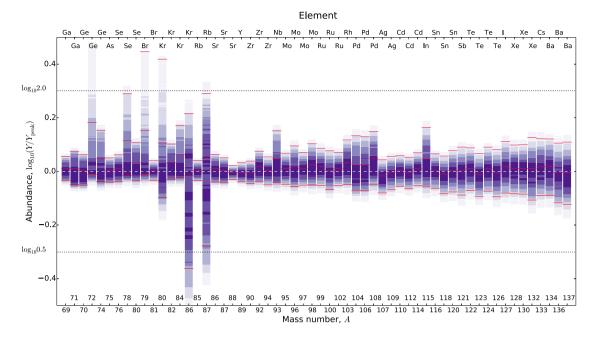


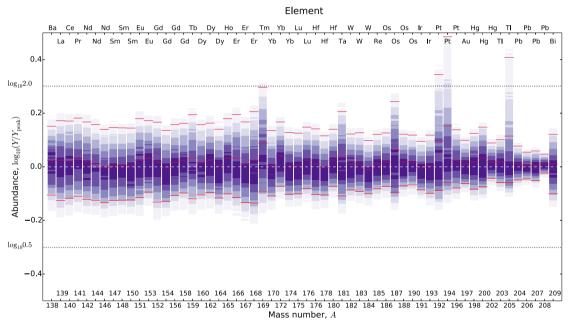
Figure 11. Same as Fig. 8 except that all the level 1 and 2 key reactions are now fixed.

0.10 0.25 0.40 0.55 0.70 0.85 1.00 Frequency, $F/F_{\rm peak}(Y)$

rates involving heavy elements listed for the 13 C-pocket conditions by Ko16 (Table B) appear as key rates for at least one nuclide in our standard 13 C-pocket case. There are special rates, neutron captures on 56 Fe, 64 Ni, and 138 Ba, which we discuss below. We did not find in our TP phase the same reactions as found by Ko16 (cf. their table A). The different methodologies and the limited cases studied are likely responsible. Nevertheless, we note that most of the reactions found by Ko16 for the TP conditions are actually key rates for the standard case or the '2 \times ¹³C' case (which correspond to higher

neutron densities compared to the standard 13 C-pocket case). The only significant rates we found in the TP condition, which are not either directly producing or destroying the nuclide in question (or very close by nuclei), are 57 Fe(n, γ) and 56 Fe(n, γ). These rates, however, only appear for one nuclide (148Nd) at level 2 so should be treated as any other level 2 key reactions (i.e. only be considered after all level 1 key rates have been improved). Finally, for the TP phase, we obtained several more β -decay reactions as key rates for the selected nuclei, compared to the 13 C-pocket conditions. How-





 $0.10 \;\; 0.25 \;\; 0.40 \;\; 0.55 \;\; 0.70 \;\; 0.85 \;\; 1.00$ Frequency, $F/F_{
m peak}(Y)$

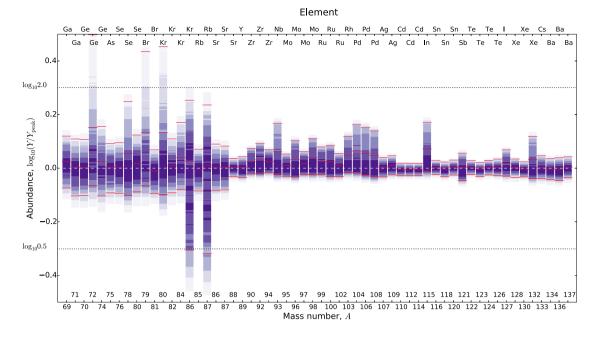
Figure 12. Total production uncertainties (same as Fig. 8) for the case with half of the standard initial 13 C abundance ('0.5 × 13 C' case).

ever, as before, most of the uncertainty in the final abundances is caused by the uncertainty in the neutron-capture rates.

3.4.1 Neutron captures on ⁵⁶Fe, ⁶⁴Ni, and ¹³⁸Ba

As explained above, in most cases, key rates dominating the nuclear uncertainties are the neutron captures either directly producing or destroying the nuclide in question. There are, however, three neutron-capture rates that play a significant role in the uncertainty

for many nuclides during the ¹³C-pocket conditions. These are the neutron-capture rates on ⁵⁶Fe, ⁶⁴Ni, and ¹³⁸Ba. Neutron-capture rates on ⁵⁶Fe, ⁶⁴Ni, and ¹³⁸Ba appear as level 2 key rates for many nuclides in Table A1. This means that for many nuclides local neutron-capture rates are still the dominant source of uncertainty but the importance of these three neutron-capture rates becomes evident by looking the correlation plots for a few key nuclides: ⁸⁸Sr (Fig. 14), ¹³⁸Ba (Fig. 15), and ²⁰⁸Pb (Fig. 16); we have selected these isotopes because they are the most abundant for the three



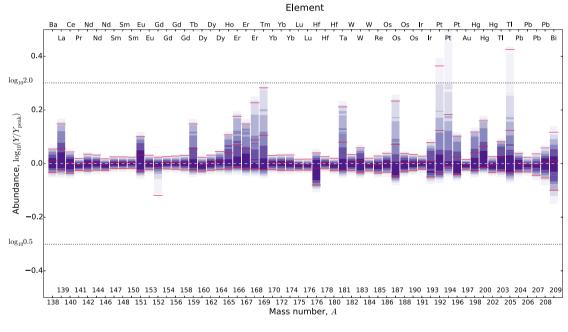


Figure 13. Total production uncertainties (same as Fig. 8) for the case with double the standard initial 13 C abundance ('2 × 13 C' case).

0.10 0.25 0.40 0.55 0.70 0.85 1.00 Frequency, $F/F_{\rm peak}(Y)$

main peaks of the s-process path. In these plots, the correlation coefficients of the 900 reactions considered are shown, and the five reactions with the highest correlations are listed. These plots explain the main reason why these two or three neutron captures are not level 1 key rates: more than one of them contributes to the total uncertainty. Indeed, it is very rare to have a strong correlation with more than one rate since correlations with different rates weaken each other. Examination of the plots reveals that for all three test nuclides, the 56 Fe(n, γ) and 64 Ni(n, γ) reactions have high correla-

tion factors, albeit they are below our threshold of 0.65. Only at the second level do they appear as key rates, but since these three reactions significantly contribute to the uncertainty of so many nuclides, it makes them priority targets for future measurements. For two of these neutron-capture reactions, the reason for their importance is clear. $^{56}\text{Fe}(n,\gamma)$ affects the neutron/seed ratio, while $^{138}\text{Ba}(n,\gamma)$ is an important bottleneck in the reaction chain. We elucidate the role of $^{64}\text{Ni}(n,\gamma)$ by presenting Fig. 17, which shows the Maxwellian averaged cross-sections (MACS) at 30 keV for a range of Ni isotopes.

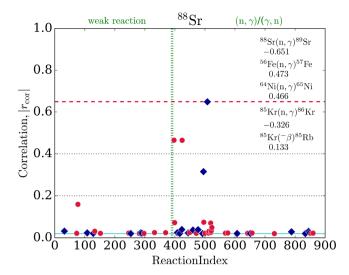


Figure 14. The correlation coefficients of reactions with respect to an abundance change of 88 Sr during the 13 C-pocket conditions. The absolute values of the coefficients are plotted against a reaction index number. Red circles stand for positive correlation and blue squares for negative correlation, respectively. Reaction indices in the range of 1–390 denote weak reactions and those in the range 391–900 identify neutron captures. The five reactions with the highest correlations are listed in the upper right corner. Note that, for better readability, reactions with correlation factors $|r_{\rm cor}| < 0.02$ are omitted from this plot.

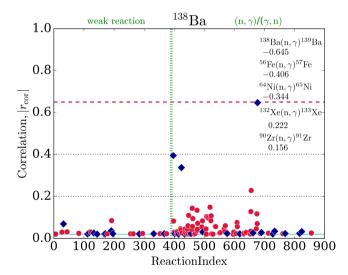


Figure 15. Same as for Fig. 14 for ¹³⁸Ba.

The even-neutron isotopes generally have smaller MACS values, reducing with increasing number of neutrons. The small value for $^{64}{\rm Ni}$ means that $^{64}{\rm Ni}$ becomes an effective bottleneck in the reaction chain towards $^{65}{\rm Cu}$ and all heavier nuclei in the s-process path. One further reaction that we highlight as being of possible interest is that of $^{140}{\rm Ce}(n,\gamma)$, which although identified only at level 3, is found to be a key rate at this level for multiple nuclei.

3.5 Comparison to the weak s-process key rates

In Table 5, we compare the correlation coefficient for the key reactions for the main s-process, which are also relevant for the weak s-process (see Nishimura et al. 2017). Not all of the latter are level 1 key rates for the weak s-process but it is interesting to know

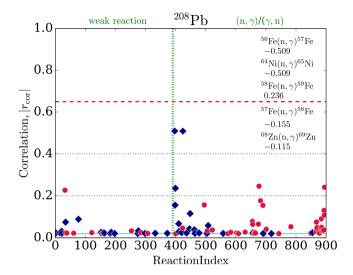


Figure 16. Same as for Fig. 14 for ²⁰⁸Pb.

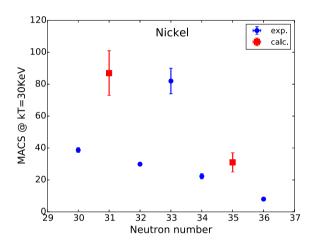


Figure 17. Maxwellian averaged cross-sections (MACS) at 30 keV for Ni isotopes (data taken by the website www.kadonis.org).

Table 5. Key rates dominating the production uncertainties for the ¹³C-pocket conditions and also important for the weak s-process (column 1), nuclide for which the rate is highly correlated during the ¹³C-pocket conditions (2), value of this correlation (3), isotopes for which the rate is correlated in the weak s-process production (4), and value of this correlation (5).

Key rates	Nuclide main s-	r _{cor,0} main s-	Nuclide weak s-	r _{cor,0} weak s-
7^{2} Ge(n, γ) 73 Ge	⁷² Ge	-0.93	⁷² Ge	-0.85
74 Ge(n, γ) 75 Ge	⁷⁴ Ge	-0.97	⁷⁴ Ge	-0.44
75 As(n, γ) 76 As	75 As	-0.86	⁷⁵ As	-0.50
78 Se(n, γ) 79 Se	⁷⁸ Se	-0.96	⁷⁸ Se	-0.71
84 Kr(n, γ) 85 Kr	⁸⁴ Kr	-0.99	⁸⁴ Kr	-0.49
85 Kr(n, γ) 86 Kr	$^{86}\mathrm{Kr}$	0.88	$^{86}\mathrm{Kr}$	0.84

which rate uncertainties affect predictions for both the main and weak s-process. In particular, $^{72}Ge(n,\gamma)^{73}Ge,\,^{78}Se(n,\gamma)^{79}Se,$ and $^{85}Kr(n,\gamma)^{86}Kr$ are key rates with very high correlations for both the main and weak s-process. Therefore, a more precise measurement of these rates will enable more precise nucleosynthesis predictions for both processes.

3.6 Opportunities for improved nuclear data

A significant number of key reactions have been identified, which thus become the focus for future experimental work. Of these, the vast majority are of (n, γ) type, with the remainder being beta-decays. By the nature of the scenario being explored, all the reactions lie along or close to the valley of stability, and consequently the targets required for (n, γ) studies are stable or long lived such that solid or gaseous targets of sufficiently rich isotopic content may be acquired.

Table A1 lists the key reactions obtained in the present MC study. Before embarking on an experimental investigation of any of the listed reactions, two issues have to be considered, which are connected to the possible impact of a measurement. The first concerns the fact that a straightforward measurement of a cross-section in the laboratory yields the cross-section for the reaction proceeding on the ground state of the target nuclei. Depending on the plasma temperature *T*, however, a considerable fraction of nuclei in a star are in excited states and reactions on those have to be predicted by theory. The ground-state contribution to the stellar rate (Rauscher 2012a.b)

$$X_0(T) = \frac{2J_0 + 1}{G(T)} \frac{\mathcal{R}_{\},f,}(T)}{\mathcal{R}^*(T)}$$
(2)

quantifies the fraction of the stellar rate which can be constrained by such a cross-section measurement. Here, J_0 is the spin of the ground state and G(T) is the nuclear partition function of the target nucleus. The reaction rate obtained by energy-averaging the ground-state cross-sections is denoted by $\mathcal{R}_{g.s.}$ and the full stellar rate, including reactions on excited states, by \mathcal{R}^* . As described in Rauscher et al. (2016), the X_0 were also used to construct the temperature dependence of the rate uncertainties. An experiment will only be able to significantly reduce uncertainties for reactions with large ground-state contributions to the stellar rate. Although the stellar temperatures encountered in the s-process are comparatively low, it has been shown in Rauscher (2012b) and Rauscher et al. (2011) that non-negligible excited-state contributions appear for a number of nuclei also in the s-process, especially in the rare-earth region.

For convenience, the ground-state contributions X_0 at two sprocess temperatures are given for each key neutron capture in Table A1. Most of the reactions have a ground-state contribution of unity, meaning a laboratory experiment may provide the relevant nuclear data.

The other issue to be considered before selecting a target for a measurement is that key rates in our definition are identified by the strength of the correlation factor, which identifies reactions that contribute most to the uncertainty of a particular nuclide's abundance relative to the contributions of all other reactions. It is important to remember that this does not indicate whether that abundance uncertainty itself is large or small, and hence whether it is of acute interest for improvement – for this, one must cross-reference with Table 3 or Fig. 8 to identify the nuclides having the largest uncertainties in their abundance. Doing so reveals where there is scope for updates to the reaction rate library to be useful. In several cases, there are already new data published or presently under analysis that are not yet included; these are detailed below. For others, new precision data are encouraged.

The Ge(n, γ) reactions have recently been subjected to measurements by the n_TOF collaboration (Lederer et al. 2014) and the data are presently being analysed. The ⁷⁸Se(n γ) reaction is the subject of a near-future study (Lederer-Woods & Murphy 2017) that is motivated in part by previous work (Nishimura et al. 2017) from this

paper's authorship. ⁷⁹Se(n γ) is a well-known branching point for the main s-process and is the topic of another near-future n_TOF study (Domingo-Pardo 2014). There are also established intentions to pursue Kr(n γ) experiments (Reifarth 2013). A n_TOF study of ⁹³Zr(n γ) is already published (Tagliente et al. 2013), but it is noted that the conclusions drawn were limited by the relatively low enrichment (c. 20 per cent) of the target that was available.

Our MC process reveals a cluster of Rh and Pd nuclides with slightly increased abundance uncertainties around mass 105; the associated level 1 key reaction rates are also identified. New experimental time of flight data for neutron captures on Pd isotopes, covering the 15–100 keV region, has been provided by Terada et al. (2014). These report uncertainties improved now to the level of <6 per cent. The data for 106 Pd are interesting as they appear to show a significant (15–22 per cent) reduction compared to previous data. 115 In has a raised abundance uncertainty, identified here as due to the uncertainty in the 115 In(n, γ) reaction rate. New data are available here also (Katabuchi et al. 2015) that show agreement with another earlier data set but which disagree (at the level of \sim 17 per cent) with other data sets and evaluations. Further clarification is required.

For the 132 Xe(n, γ) reaction, the accepted rate is based on the activation study of Beer (1991) that has an experimental uncertainty \sim 8.5 per cent in the neutron capture cross-section at $kT=30\,\mathrm{keV}$. In the case of the 159 Tb(n, γ) reaction, the reaction rate used here, and its uncertainty, is based on an average of the ENDFB71 and JENDL40 evaluated libraries, which in turn are based on several data sets that themselves show some disagreement (see e.g. Lepine, Douglas & Maia 1972; Mizumoto, Macklin & Halperin 1978). The 166 Er, 168 Er, and 169 Tm(n, γ) reactions see a similar situation. Precision neutron capture data are needed.

Laboratory measurements of neutron capture cross-sections are typically constrained to investigation of capture to ground states. Consequently, despite precision measurements, the possibility of capture on thermally excited states leads to overall greater uncertainties. Such is the case for the $^{169}\mathrm{Tm}(n,\gamma)$, $^{181}\mathrm{Ta}(n,\gamma)$, and $^{187}\mathrm{Os}(n,\gamma)$ reactions that are identified as the level 1 key rates responsible for the increased uncertainties in the $^{169}\mathrm{Tm}$, $^{181}\mathrm{Ta}$, and $^{187}\mathrm{Os}$ abundances. Despite relatively well-measured neutron capture cross-sections, excited states at 8.4, 6.2, and 9.8 keV, respectively, lead to the abundance variations seen in the current study that will be hard to improve upon by experiment.

Three other nuclides are determined to have poorly constrained abundances: $^{192,\,194}Pt$ and ^{205}Pb . The reaction rate library used throughout this study provides only theoretical rates for the associated key reactions, for which our approach has been to consistently assign an uncertainty factor of 2. In fact, recent experimental data now exist for the $^{192,\,194}Pt(n,\gamma)$ level 1 key rates (Koehler & Guber 2013) and thus the new abundance uncertainties for $^{192,\,194}Pt$ are expected to best represented by Fig. 10. This provides a useful illustration of the improvement that new data can provide.

Several further reactions are of particular interest because of their broader impact: $^{56}{\rm Fe}(n\,\gamma),\,^{64}{\rm Ni}(n\,\gamma),\,^{138}{\rm Ba}(n\,\gamma),\,$ and $^{140}{\rm Ce}(n\,\gamma)$ are identified as level 2 and 3 reactions for a large number of nuclear abundances. For the first of these, there are a number of published data sets (Macklin, Pasma & Gibbons 1964; Allen et al. 1976, 1982; Wang et al. 2010), resulting in an uncertainty of around 10 per cent, but given the role of neutron capture on seed $^{56}{\rm Fe}$ nuclei in this and other nucleosynthesis environments, greater precision is still needed. For the $^{64}{\rm Ni}(n\,\gamma)$ reaction, a recent measurement of the thermal neutron capture cross-section has been made (Shivashankar

et al. 2016) and an experiment is approved at the n_TOF facility (Tain et al. 2006). In the case of $^{138} Ba(n\,\gamma)$, Heil et al. (2005), using the $^{18} O(p,n)$ reaction that produces neutrons with a 5 keV thermal energy distribution, measured the Maxwellian-averaged neutron capture cross-section to a precision of about 4 per cent, in fair agreement with previous work (Beer, Corvi & Mutti 1997). The neutron capture on $^{140} Ce$ will be the subject of another near-future n_TOF measurement (Amaducci 2018). Its cross-section, in fact, albeit having been precisely measured at 25 keV (Käppeler et al. 1996), needs more precise data at lower energies, where the dominant resonance at 2.5 keV is poorly constrained.

Further experimental progress is anticipated thanks to new and planned facilities. At CERN, the second experimental area at n_TOF (Weiss et al. 2015) has a shorter flight path to deliver higher neutron fluxes, while the FRANZ (Alzubaidi et al. 2016) facility at the University of Frankfurt (Germany) and SARAF (Mardor & GuberBerkovits 2013) at the Soreq research centre (Israel) should soon deliver significantly higher fluxes, and thus sensitivity and precision.

4 CONCLUSIONS

For the first time we have performed a comprehensive, large-scale MC study for the main s-process in low-mass stars, varying reactions on targets from Fe to Bi. Temperature-dependent stellar reaction rate uncertainties were individually assigned to the reactions, allowing a quantification of the uncertainties in final abundances.

We found that β -decay rate uncertainties affect only a few nuclei near s-process branchings, whereas most of the uncertainty in the final abundances is caused by uncertainties in neutron-capture rates either directly producing or destroying the nuclide of interest. Combined total nuclear uncertainties due to reactions on heavy elements are in general small (less than 50 per cent). This means that nuclear uncertainties for the main s-process will be dominated by uncertainties in well-known reactions involving light elements, such as neutron source, e.g. 13 C(α ,n) 16 O, and neutron poisons.

We studied the dependence of the uncertainties and key rates on the astrophysical conditions found in stars of different masses or metallicities (neutron-to-seed ratio) by varying the initial abundance of ¹³C. We found that the key reaction list established is relevant for the full range of conditions studied. We compared our results and method to past sensitivity studies focusing on the main s-process, in particular the comprehensive study of Koloczek et al. (2016). Our approach clearly determines the key rates that dominate the total uncertainties in the nucleosynthesis predictions (rather than showing that a reaction has an impact on a certain number of nuclides). This is important to ensure that the (re-)measurement of a key rate will significantly reduce the uncertainties in the final abundances. While the strongest globally affecting reactions found by Ko16 are almost all identified as key rates for a few nuclides, they only dominate the total uncertainties for a few nuclides. The main exceptions are three key reactions which stand out because they significantly affect the uncertainties of a larger number of nuclides. These are 56 Fe(n, γ), 64 Ni(n, γ), and 138 Ba(n, γ). Improved data for these reactions will lead to a strong global reduction in prediction uncertainties.

We also compared our key reaction list to the one we determined for the weak s-process (Nishimura et al. 2017). In particular, 72 Ge(n, γ) 73 Ge, 78 Se(n, γ) 79 Se, and 85 Kr(n, γ) 86 Kr are key rates with very high correlations for both the main and weak s-process. Therefore, a more precise measurement of these rates will enable more precise nucleosynthesis predictions for both processes.

Finally, we discussed the prospect of reducing uncertainties in the key reactions identified in this study with future experiments. Since the key rates are for nuclides along the valley of stability, many have already been measured, which explains the small total uncertainties. Nevertheless, new improved measurements are feasible and several are already underway.

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APPENDIX: KEY RATES FOR DOUBLE AND HALF OF THE INITIAL ¹³C ABUNDANCE

As explained in Section 3.3, the tables in this Appendix are provided to assess the sensitivity of the key rate list to the astrophysical conditions. We list in Table A1, the key rates for the 'standard' $^{13}\mathrm{C}$ -pocket case and the corresponding total uncertainties are shown in Fig. 8. In Table A2, we list the key rates for the '0.5 \times $^{13}\mathrm{C}$ ' case and the corresponding total uncertainties are shown in Fig. 12. Similarly, in Table A3, we list the key rates for the '2 \times $^{13}\mathrm{C}$ ' case and the corresponding total uncertainties are shown in Fig. 13. The reference key reaction list is that of the 'standard' case given in Table A1. The other two tables are presented for discussion and reference only and should not be used to extract key rates. Finally, in Table A4, the key rates for the TP phase are presented and the corresponding total uncertainties are shown in Fig. 9.

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Table A1. The key reaction rates for the standard model. Key rates in levels 1-3 are shown, along with their correlation factors r_{cor0} , r_{cor1} , and r_{cor2} , respectively. Not all s-process nuclides analysed are listed but only those for which key rates were found. Also shown for each rate are the ground state contributions X_0 to the stellar rate of the (n, γ) reaction and uncertainty factors of the β -decay rate at two plasma temperatures, respectively.

Nuclide	$r_{\rm cor,0}$	$r_{\rm cor,1}$	$r_{\rm cor,2}$	Key rate Level 1	Key rate Level 2	Key rate Level 3	X_0 (8, 30 keV)	Weak rate uncertainty factor (8, 30 keV)
⁶⁹ Ga	-0.77			⁶⁹ Ga(n, γ) ⁷⁰ Ga			1.00, 1.00	
	-0.34	-0.67			64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁷¹ Ga	-0.89			71 Ga(n, γ) 72 Ga			1.00, 1.00	
⁷⁰ Ge	-0.87			70 Ge(n, γ) 71 Ge			1.00, 1.00	
	-0.27	-0.66			64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁷² Ge	-0.93			72 Ge(n, γ) 73 Ge			1.00, 1.00	
⁷⁴ Ge	-0.97			74 Ge(n, γ) 75 Ge			1.00, 1.00	
75 As	-0.86			75 As(n, γ) 76 As			1.00, 1.00	
⁷⁶ Se	-0.89			76 Se(n, γ) 77 Se			1.00, 1.00	
⁷⁸ Se	-0.97			78 Se(n, γ) 79 Se			1.00, 1.00	
⁸⁰ Se	-0.96			80 Se(n, γ) 81 Se			1.00, 1.00	
⁷⁹ Br	-0.94			79 Se(n, γ) 80 Se			1.00, 1.00	
⁸¹ Br	-0.74			81 Br(n, γ) 82 Br			1.00, 1.00	
80 Kr	-0.90			79 Se(n, γ) 80 Se			1.00, 1.00	
	0.24	<u>0.85</u>			79 Se(β^{-}) 79 Br			1.30, 1.49
⁸² Kr	-0.97			82 Kr(n, γ) 83 Kr			1.00, 1.00	
⁸⁴ Kr	-0.98			84 Kr(n, γ) 85 Kr			1.00, 1.00	
⁸⁶ Kr	0.88			85 Kr(n, γ) 86 Kr			1.00, 1.00	
	-0.43	-0.95			$^{85}{\rm Kr}(\beta^-)^{85}{\rm Rb}$			1.30, 1.30
	-0.12	-0.28	-1.00			86 Kr(n, γ) 87 Kr	1.00, 1.00	
⁸⁵ Rb	-0.86			85 Rb(n, γ) 86 Rb			1.00, 1.00	
⁸⁷ Rb	0.86			85 Kr(n, γ) 86 Kr			1.00, 1.00	
	-0.41	-0.85			$^{85}{\rm Kr}(\beta^-)^{85}{\rm Rb}$			1.30, 1.30
	0.20	0.39	0.77			86 Kr(n, $\gamma)^{87}$ Kr	1.00, 1.00	
⁸⁶ Sr	-0.94			86 Sr(n, γ) 87 Sr			1.00, 1.00	
⁸⁷ Sr	-0.92			87 Sr(n, γ) 88 Sr			1.00, 1.00	
⁸⁸ Sr	-0.65			88 Sr(n, γ) 89 Sr			1.00, 1.00	
	0.47	0.69			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
	0.47	0.68			64 Ni(n, γ) 65 Ni		1.00, 1.00	
0.0	0.06	0.11	<u>0.65</u>	00 00		58 Fe(n, $\gamma)^{59}$ Fe	1.00, 1.00	
⁸⁹ Y	-0.83			89 Y(n, γ) 90 Y			1.00, 1.00	
	0.33	<u>0.67</u>			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
	0.34	0.68			64 Ni(n, γ) 65 Ni	50 50	1.00, 1.00	
00-	0.07	0.15	0.67	00 01-		58 Fe(n, γ) 59 Fe	1.00, 1.00	
90 Zr	$\frac{-0.89}{}$			90 Zr(n, γ) 91 Zr	64		1.00, 1.00	
02-	0.28	0.68		02- 4 02-	64 Ni(n, γ) 65 Ni		1.00, 1.00	
92 Zr	-0.92			92 Zr(n, γ) 93 Zr	(4		1.00, 1.00	
04-	0.22	<u>0.67</u>		04	64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁹⁴ Zr	$\frac{-0.86}{0.000}$			94 Zr(n, γ) 95 Zr	64		1.00, 1.00	
03	0.30	0.65		93 >94	64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁹³ Nb	$\frac{-0.97}{0.14}$	0.67		93 Zr(n, γ) 94 Zr	6/21:/ \6521:		1.00, 1.00	
⁹⁵ Mo	0.14	<u>0.67</u>		⁹⁵ Mo(n, γ) ⁹⁶ Mo	64 Ni(n, γ) 65 Ni		1.00, 1.00	
Mo	$\frac{-0.85}{0.20}$	0.65		3 Mo(n, γ) 3 Mo	⁶⁴ Ni(n, γ) ⁶⁵ Ni		1.00, 1.00	
⁹⁶ Mo	0.29	<u>0.65</u>		96 N. J () 97 N. J	$^{\circ}$ Ni(n, γ) $^{\circ\circ}$ Ni		1.00, 1.00	
⁹⁷ Mo	$\frac{-0.94}{0.97}$			96 Mo(n, γ) 97 Mo 97 Mo(n, γ) 98 Mo			1.00, 1.00	
⁹⁸ Mo	$\frac{-0.87}{0.04}$			$^{98}\text{Mo(n, }\gamma)^{99}\text{Mo}$			1.00, 1.00	
⁹⁹ Ru	$\frac{-0.94}{0.01}$			99 Tc(n, γ) 100 Tc			1.00, 1.00	
¹⁰⁰ Ru	$\frac{-0.91}{0.02}$			100 Ru(n, γ) 101 Ru			1.00, 1.00	
¹⁰² Ru	$\frac{-0.93}{0.96}$			102 Ru(n, γ) 103 Ru			1.00, 1.00	
¹⁰³ Rh	$\frac{-0.86}{0.05}$			103 Rh(n, γ) 104 Rh			1.00, 1.00	
¹⁰⁴ Pd	$\frac{-0.95}{0.07}$			$^{104}\text{Pd}(n, \gamma)^{105}\text{Pd}$			0.95, 0.80	
¹⁰⁶ Pd	$\frac{-0.97}{0.07}$			$^{106}\text{Pd}(n, \gamma)^{107}\text{Pd}$			1.00, 1.00	
¹⁰⁸ Pd	$\frac{-0.97}{0.06}$			$^{108}\text{Pd}(n, \gamma)^{107}\text{Pd}$			1.00, 1.00	
¹⁰⁷ Ag	$\frac{-0.96}{0.81}$			$^{107}\text{Pd}(n, \gamma)^{108}\text{Pd}$			1.00, 1.00	
109 Ag	$\frac{-0.81}{0.80}$			109 Ag(n, γ) 110 Ag			1.00, 1.00	
110 Ag	$\frac{-0.80}{0.41}$	0.40	0.71	$Ag(\Pi, \gamma)^{110}Ag$		110 Cd(n, γ) 111 Cd	1.00, 1.00	
¹¹² Cd	-0.41 -0.40	-0.48 -0.45	$\frac{-0.71}{-0.69}$			$^{112}\text{Cd}(n, \gamma)^{113}\text{Cd}$	1.00, 1.00 1.00, 1.00	
¹¹⁴ Cd	-0.40 -0.36	-0.43 -0.43	$\frac{-0.69}{-0.65}$			$^{114}\text{Cd}(n, \gamma)^{115}\text{Cd}$	1.00, 1.00	
¹¹⁵ In	-0.36 -0.97	-0.43	-0.03	115 In(n, γ) 116 In		Cu(II, γ) Cd	1.00, 1.00	
111	<u>-0.97</u>			$m(n, \gamma)$ III			1.00, 1.00	

Table A1 - continued

Nuclide	$r_{\rm cor,0}$	$r_{\rm cor,1}$	$r_{\rm cor,2}$	Key rate Level 1	Key rate Level 2	Key rate Level 3	X_0 (8, 30 keV)	Weak rate uncertainty factor (8, 30 keV)
116Sn	-0.51	-0.58	-0.78			116 Sn(n, γ) 117 Sn	1.00, 1.00	·
¹¹⁸ Sn	-0.51 -0.59	-0.67	_0.76		118 Sn(n, γ) 119 Sn	3π(π, γ) 3π	1.00, 1.00	
¹²⁰ Sn	-0.57	$\frac{-0.67}{-0.67}$			120 Sn(n, γ) 121 Sn		1.00, 1.00	
¹²¹ Sb	-0.97	<u>-0.07</u>		121 Sb(n, γ) 122 Sb	3π(π, γ) 3π		0.98, 0.93	
¹²⁴ Te	$\frac{-0.52}{-0.53}$	-0.65	-0.76	30(II, y) 30		$^{124}\text{Te}(n, \gamma)^{125}\text{Te}$	1.00, 1.00	
¹²⁶ Te	-0.69	0.05		$^{126}\text{Te}(n, \gamma)^{127}\text{Te}$		re(n, y) re	1.00, 1.00	
¹²⁷ I	$\frac{-0.02}{-0.92}$			$^{127}I(n, \gamma)^{128}I$			1.00, 1.00	
¹²⁸ Xe	0.66			$^{128}I(\beta^{-})^{128}Xe$			1.00, 0.55	1.64, 5.42
¹³⁰ Xe	-0.57	-0.71		$I(p^{-})$ Nc	130 Xe(n, γ) 131 Xe		1.00, 1.00	1.04, 5.42
¹³² Xe	-0.97			132 Xe(n, γ) 133 Xe	$\mathcal{H}\mathbf{c}(\mathbf{n}, \gamma)$		1.00, 1.00	
¹³³ Cs	$\frac{0.57}{-0.89}$			133 Cs(n, γ) 134 Cs			1.00, 1.00	
¹³⁴ Ba	$\frac{-0.85}{-0.85}$			134 Ba(n, γ) 135 Ba			1.00, 1.00	
¹³⁶ Ba	$\frac{-0.83}{-0.88}$			136 Ba(n, γ) 137 Ba			1.00, 1.00	
¹³⁷ Ba	$\frac{-0.88}{-0.84}$			137 Ba(n, γ) 138 Ba			1.00, 1.00	
¹³⁸ Ba	$\frac{-0.64}{-0.65}$	0.72		$Da(n, \gamma)$ Da	138 Ba(n, γ) 139 Ba		1.00, 1.00	
139 La	-0.03 -0.87	-0.73		139 La(n, γ) 140 La	$\mathbf{Da}(\mathbf{n}, \gamma) = \mathbf{Da}$		1.00, 1.00	
La		0.92		La(II, γ) La	138 Ba(n, γ) 139 Ba			
¹⁴⁰ Ce	0.36	$\frac{0.83}{0.65}$			138 Ba(n, γ) 139 Ba		1.00, 1.00	
· ···Ce	0.59	0.65	0.00		$\operatorname{Da}(\Pi, \gamma)^{\operatorname{res}}\operatorname{Da}$	140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁴¹ Pr	-0.39	-0.42	-0.90		138 Ba(n, γ) 139 Ba	$Ce(n, \gamma)$	1.00, 1.00	
· · · PT	0.59	$\frac{0.65}{0.33}$	0.05		130 Ba(n, γ) 135 Ba	140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁴² Nd	0.31	0.33	0.85			142 Nd(n, γ) 143 Nd	1.00, 1.00	
146 Nd	-0.31	-0.34	$\frac{-0.67}{0.76}$				1.00, 1.00	
147 Sm	0.28	0.30	0.76			140 Ce(n, γ) 141 Ce	1.00, 1.00	
148 Sm	0.28	0.30	0.74			140 Ce(n, γ) 141 Ce	1.00, 1.00	
	0.28	0.29	0.74			140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁵⁰ Sm	0.28	0.29	0.76	151 152		140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁵¹ Eu	$\frac{-0.70}{0.10}$			151 Eu(n, γ) 152 Eu		140 141	0.89, 0.79	
152	0.19	0.29	0.68			140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁵² Gd	0.59	0.61	0.79			$^{151}\text{Sm}(\beta^-)^{151}\text{Eu}$		3.60, 5.42
¹⁵⁴ Gd	0.27	0.29	0.71			140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁵⁶ Gd	0.27	0.28	0.67	150 160		140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁵⁹ Tb	-0.79			159 Tb(n, γ) 160 Tb		140	1.00, 0.98	
	0.16	0.29	0.74			140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁶⁴ Dy	-0.35	-0.38	-0.71			164 Dy(n, γ) 165 Dy	1.00, 0.97	
¹⁶⁵ Ho	-0.68			$^{165}{\rm Ho}({\rm n},\gamma)^{166}{\rm Ho}$			1.00, 1.00	
	0.19	0.28	0.72			140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁶⁶ Er	-0.81			166 Er(n, $\gamma)^{167}$ Er			1.00, 0.98	
	0.15	0.28	0.72			140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁶⁷ Er	-0.78			167 Er(n, $\gamma)^{168}$ Er			1.00, 1.00	
	0.17	0.28	0.72			140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁶⁸ Er	-0.86			168 Er(n, $\gamma)^{169}$ Er			1.00, 0.98	
	0.11	0.28	0.72			140 Ce(n, γ) 141 Ce	1.00, 1.00	
$^{169}\mathrm{Tm}$	-0.90			169 Tm(n, γ) 170 Tm			0.51, 0.42	
	0.10	0.28	0.71			140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁷⁵ Lu	0.26	0.27	0.69			140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁷⁶ Lu	0.25	0.26	0.65			140 Ce(n, γ) 141 Ce	1.00, 1.00	
¹⁷⁶ Hf	0.61	0.63	0.89			176 Lu(β^{-}) 176 Hf		1.30, 1.33
¹⁸¹ Ta	-0.84		_	181 Ta $(n, \gamma)^{182}$ Ta			0.61, 0.55	
	0.12	0.26	0.67			140 Ce(n, γ) 141 Ce	1.00, 1.00	
^{183}W	-0.49	-0.51	-0.82			183 W(n, γ) 184 W	0.99, 0.93	
¹⁸⁷ Os	-0.86			187 Os(n, γ) 188 Os			0.57, 0.46	
¹⁸⁸ Os	-0.34	-0.35	-0.67			188 Os(n, γ) 189 Os	1.00, 1.00	
¹⁹³ Ir	-0.58	-0.59	-0.84			193 Ir(n, γ) 194 Ir	1.00, 0.99	
¹⁹² Pt	-0.89			192 Pt(n, γ) 193 Pt			1.00, 1.00	
¹⁹⁴ Pt	$\frac{-0.90}{-0.90}$			194 Pt $(n, \gamma)^{195}$ Pt			1.00, 1.00	
¹⁹⁶ Pt	$\frac{0.56}{-0.63}$	-0.65	-0.89	· (, / /		196 Pt(n, γ) 197 Pt	1.00, 1.00	
¹⁹⁸ Hg	-0.63	-0.65			198 Hg(n, γ) 199 Hg	(, / /	1.00, 1.00	
²⁰⁰ Hg	-0.67			200 Hg(n, γ) 201 Hg	0(, / / 116		1.00, 1.00	
²⁰³ Tl	$\frac{0.07}{-0.48}$	-0.49	-0.78			203 Tl(n, γ) 204 Tl	1.00, 1.00	
²⁰⁵ Tl	<u>-0.87</u>	0.77		205 Pb $(n, \gamma)^{206}$ Pb		11(11, 1/) 11	0.83, 0.82	
²⁰⁹ Bi	0.53	0.56	0.71	10(11, 7) 10		208 Pb(n, $\gamma)^{209}$ Pb	1.00, 1.00	

Table A2. Key reaction rates for the model with half the initial 13 C abundance ('0.5 × 13 C' case). Key rates in levels 1–3 are shown, along with their correlation factors r_{cor0} , r_{cor1} , and r_{cor2} , respectively. Not all s-process nuclides analysed are listed but only those for which key rates were found. Also shown for each rate are the ground-state contributions of the (n,γ) reaction to the stellar rate and uncertainty factors of the β-decay rate at two plasma temperatures, respectively.

Nuclide	$r_{\rm cor,0}$	$r_{\rm cor,1}$	$r_{\rm cor,2}$	Key rate Level 1	Key rate Level 2	Key rate Level 3	X_0 (8, 30 keV)	β -decay
⁹ Ga	-0.88			⁶⁹ Ga(n, γ) ⁷⁰ Ga			1.00, 1.00	
	0.33	0.73			56 Fe(n, γ) 57 Fe		1.00, 1.00	
	0.29	0.65			64 Ni(n, γ) 65 Ni		1.00, 1.00	
^l Ga	-0.93			71 Ga(n, γ) 72 Ga			1.00, 1.00	
	0.26	0.72			56 Fe(n, γ) 57 Fe		1.00, 1.00	
	0.25	0.67			64 Ni(n, γ) 65 Ni		1.00, 1.00	
	0.04	0.12	0.72			58 Fe(n, γ) 59 Fe	1.00, 1.00	
)Ge	-0.92			70 Ge(n, γ) 71 Ge			1.00, 1.00	
	0.25	0.73			56 Fe(n, γ) 57 Fe		1.00, 1.00	
	0.25	0.66			64 Ni(n, γ) 65 Ni		1.00, 1.00	
	0.05	0.11	0.67			58 Fe(n, $\gamma)^{59}$ Fe	1.00, 1.00	
² Ge	-0.93			72 Ge(n, γ) 73 Ge			1.00, 1.00	
	0.06	0.71			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
	0.06	0.67			64 Ni(n, γ) 65 Ni	#0 #0	1.00, 1.00	
	0.02	0.14	0.76			58 Fe(n, $\gamma)^{59}$ Fe	1.00, 1.00	
⁴ Ge	-0.96	-0.96			74 Ge(n, γ) 75 Ge	#0 #0	1.00, 1.00	
_	0.05	0.06	0.73			58 Fe(n, γ) 59 Fe	1.00, 1.00	
⁵ As	-0.83			75 As(n, γ) 76 As			1.00, 1.00	
	0.37	0.69			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
	0.36	0.68			64 Ni(n, γ) 65 Ni	#0 #0	1.00, 1.00	
	0.10	0.18	0.73			58 Fe(n, $\gamma)^{59}$ Fe	1.00, 1.00	
⁶ Se	-0.86			76 Se(n, γ) 77 Se	56 57		1.00, 1.00	
	0.35	0.69			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
	0.34	0.68			64 Ni(n, γ) 65 Ni	#0 #0	1.00, 1.00	
0	0.11	0.19	0.71	70 70		58 Fe(n, $\gamma)^{59}$ Fe	1.00, 1.00	
⁸ Se	-0.97			78 Se(n, γ) 79 Se	56 57		1.00, 1.00	
	0.12	0.67			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
	0.12	0.68			64 Ni(n, γ) 65 Ni	#0 #0	1.00, 1.00	
0	0.05	0.21	<u>0.67</u>	00 01		58 Fe(n, γ) 59 Fe	1.00, 1.00	
⁰ Se	-0.91			80 Se(n, γ) 81 Se	61 65		1.00, 1.00	
0	0.25	0.66		70 00	64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁹ Br	-0.94			79 Se(n, γ) 80 Se	61 65		1.00, 1.00	
.1	0.05	0.65			64 Ni(n, γ) 65 Ni	91 92	1.00, 1.00	
¹ Br	-0.58	-0.59	-0.83	70		81 Br(n, γ) 82 Br	1.00, 1.00	
⁰ Kr	-0.90			79 Se(n, γ) 80 Se	70 70		1.00, 1.00	
2	0.25	0.80		02 02	79 Se(β^{-}) 79 Br			1.30, 1.49
² Kr	-0.91			82 Kr(n, γ) 83 Kr	64		1.00, 1.00	
4	0.25	0.66		0.4	64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁴ Kr	-0.96			84 Kr(n, γ) 85 Kr	64 65		1.00, 1.00	
6	0.17	0.65		0506	64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁶ Kr	0.88			85 Kr(n, γ) 86 Kr	0505		1.00, 1.00	
	-0.43	$\frac{-0.97}{0.000}$			$^{85}{ m Kr}(eta^-)^{85}{ m Rb}$	96 , 97		1.30, 1.30
5 . .	-0.07	-0.12	-0.93	05-1 . 06-1		86 Kr(n, γ) 87 Kr	1.00, 1.00	
⁵ Rb	-0.66			85 Rb(n, γ) 86 Rb	64		1.00, 1.00	
7	0.47	0.65		0506	64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁷ Rb	0.84			85 Kr(n, γ) 86 Kr	05 05		1.00, 1.00	
	-0.42	-0.82			85 Kr(β^{-}) 85 Rb	97		1.30, 1.30
c	0.24	0.48	0.88	06 07		86 Kr(n, γ) 87 Kr	1.00, 1.00	
Sr	-0.85			86 Sr(n, γ) 87 Sr			1.00, 1.00	
Sr	$\frac{-0.81}{0.000}$			$^{87}Sr(n, \gamma)^{88}Sr$			1.00, 1.00	
⁹ Y	$\frac{-0.69}{0.72}$			89 Y(n, γ) 90 Y			1.00, 1.00	
⁰ Zr	$\frac{-0.73}{0.70}$			90 Zr(n, γ) 91 Zr			1.00, 1.00	
² Zr	$\frac{-0.79}{0.57}$	0.71		92 Zr(n, γ) 93 Zr	947 ()957		1.00, 1.00	
⁴ Zr	-0.57	-0.71		03	94 Zr(n, γ) 95 Zr		1.00, 1.00	
³ Nb	$\frac{-0.92}{0.000}$			93 Zr(n, γ) 94 Zr	05		1.00, 1.00	
⁵ Mo	-0.64	-0.76		963	95 Mo(n, γ) 96 Mo		1.00, 1.00	
⁶ Mo	$\frac{-0.81}{0.25}$	0		96 Mo(n, γ) 97 Mo	56 57		1.00, 1.00	
7	-0.25	-0.65		07.	56 Fe(n, γ) 57 Fe		1.00, 1.00	
⁷ Mo	$\frac{-0.65}{0.24}$	0.7-		97 Mo(n, γ) 98 Mo	560 ()57-		1.00, 1.00	
	-0.34	-0.65			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	

Table A2 - continued

Nuclide	$r_{\rm cor,0}$	$r_{\rm cor,1}$	$r_{\rm cor,2}$	Key rate Level 1	Key rate Level 2	Key rate Level 3	X_0 (8, 30 keV)	β -decay
⁸ Mo	_0.79			⁹⁸ Mo(n, γ) ⁹⁹ Mo			1.00, 1.00	
	-0.29	-0.67			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
Ru	-0.71			99 Tc(n, γ) 100 Tc			1.00, 1.00	
110	$\frac{-0.71}{-0.33}$	-0.67		10(11, 7)	56 Fe(n, γ) 57 Fe		1.00, 1.00	
⁰⁰ Ru	-0.73	0.07		¹⁰⁰ Ru(n,	10(n, y) 10		1.00, 1.00	
IXu				γ) ¹⁰¹ Ru			1.00, 1.00	
	-0.32	<u>-0.68</u>		γ) Ku	56 Fe(n, γ) 57 Fe		1.00, 1.00	
² Ru	-0.52 -0.57				102 Ru(n, γ) 103 Ru			
Ru ³ Rh		-0.68		¹⁰³ Rh(n,	Ku(II, γ) Ku		1.00, 1.00	
Kn	-0.79			γ) ¹⁰⁴ Rh			0.95, 0.80	
	0.20	0.60		γ)***KII	56 Fe(n, γ) 57 Fe		1.00 1.00	
⁴ Pd	-0.29	-0.69		104 Pd(n, γ) 105 Pd	$re(n, \gamma)$ re		1.00, 1.00	
'Pd	$\frac{-0.86}{0.26}$	0.60		$^{104}Pd(n, \gamma)^{103}Pd$	56 ()57		1.00, 1.00	
c	-0.26	-0.69		106-11 107-1	56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
⁵ Pd	-0.85			$^{106}\text{Pd}(n, \gamma)^{107}\text{Pd}$	57		1.00, 1.00	
	-0.26	-0.70		100 100	56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
⁸ Pd	-0.83			$^{108}\text{Pd}(n, \gamma)^{109}\text{Pd}$			1.00, 1.00	
_	-0.30	-0.70			56 Fe(n, $\gamma)^{57}$ Fe	405	1.00, 1.00	
⁷ Ag	-0.48	-0.58	-0.84			$^{107}\text{Pd}(n, \gamma)^{108}\text{Pd}$	1.00, 1.00	
⁹ Ag	-0.46	-0.56	-0.82			109 Ag(n, γ) 110 Ag	1.00, 1.00	
⁰ Cd	-0.52	-0.69			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
² Cd	-0.53	-0.70			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
⁴ Cd	-0.54	-0.71			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
5In	-0.83			115 In(n, γ) 116 In			1.00, 1.00	
	-0.30	-0.71		· · · · ·	56 Fe(n, γ) 57 Fe		1.00, 1.00	
⁶ Sn	-0.55	$\frac{-0.70}{-0.70}$			56 Fe(n, γ) 57 Fe		1.00, 1.00	
⁸ Sn	-0.57	$\frac{0.70}{-0.70}$			56 Fe(n, γ) 57 Fe		1.00, 1.00	
⁰ Sn	-0.59	$\frac{-0.76}{-0.71}$			56 Fe(n, γ) 57 Fe		1.00, 1.00	
1Sb	-0.59 -0.50	$\frac{-0.71}{-0.55}$	0.82		$\Gamma((n, \gamma))$	121 Sb(n, γ) 122 Sb	0.98, 0.93	
² Te			-0.83		56 Fe(n, γ) 57 Fe	$SO(\Pi, \gamma)$ SO		
³ Te	-0.60	$\frac{-0.71}{0.71}$			56 Fe(n, γ) 57 Fe		1.00, 1.00	
⁴ Te	-0.59	$\frac{-0.71}{0.71}$					1.00, 1.00	
	-0.60	-0.71			56 Fe(n, γ) 57 Fe		1.00, 1.00	
⁶ Te	-0.60	-0.70			56 Fe(n, $\gamma)^{57}$ Fe	127- 129-	1.00, 1.00	
⁷ I	-0.44	-0.47	-0.77			$^{127}I(n, \gamma)^{128}I$	1.00, 0.99	
⁸ Xe	-0.59	-0.68			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
⁰ Xe	-0.61	-0.70			56 Fe(n, γ) 57 Fe		1.00, 1.00	
² Xe	-0.53	-0.55	-0.81			132 Xe(n, γ) 133 Xe	1.00, 1.00	
³ Cs	-0.58	-0.65			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
⁴ Ba	-0.60	-0.66			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
⁶ Ba	-0.60	-0.66			56 Fe(n, γ) 57 Fe		1.00, 1.00	
⁷ Ba	-0.60	-0.66			56 Fe(n, $\gamma)^{57}$ Fe		1.00, 1.00	
⁸ Ba	-0.62	-0.66			56 Fe(n, γ) 57 Fe		1.00, 1.00	
9Tb	-0.54	$\frac{-0.58}{-0.58}$	-0.72			159 Tb(n, γ) 160 Tb	1.00, 0.98	
⁶ Er	-0.59	-0.63	$\frac{0.72}{-0.76}$			166 Er(n, γ) 167 Er	1.00, 0.98	
⁷ Er	-0.55	-0.59	$\frac{0.78}{-0.73}$			167 Er(n, γ) 168 Er	1.00, 1.00	
8Er	-0.68	0.37		168 Er(n, $\gamma)^{169}$ Er		Δ1(II, γ) LI	1.00, 1.00	
9Tm	$\frac{-0.08}{-0.77}$			169Tm(n,			0.51, 0.42	
1111	<u>-0.77</u>			γ) ¹⁷⁰ Tm			0.31, 0.42	
¹ Ta	0.74						0.61.055	
	$\frac{-0.74}{0.81}$			181 Ta(n, γ) 182 Ta			0.61, 0.55	
⁷ Os	-0.81			¹⁸⁷ Os(n,			0.57, 0.46	
³ Ir	0.55	0.70	0.70	γ) ¹⁸⁸ Os		193+ / 194+	1 00 0 00	
	-0.55	-0.59	-0.70	102 p. (102 =		193 Ir(n, γ) 194 Ir	1.00, 0.99	
² Pt	$\frac{-0.88}{0.000}$			192 Pt(n, γ) 193 Pt			1.00, 1.00	
Pt	-0.89			194 Pt(n, γ) 195 Pt			1.00, 1.00	
Pt	-0.65			196 Pt(n, γ) 197 Pt			1.00, 1.00	
⁸ Hg	-0.66			¹⁹⁸ Hg(n,			1.00, 1.00	
				γ) ¹⁹⁹ Hg				
⁰ Hg	-0.76			²⁰⁰ Hg(n,			1.00, 1.00	
				γ) ²⁰¹ Hg				
³ Tl	-0.66			203 Tl(n, γ) 204 Tl			1.00, 1.00	
⁵ Tl	$\frac{-0.92}{-0.92}$			205 Pb $(n, \gamma)^{206}$ Pb			0.83, 0.82	
⁷ Pb	$\frac{-0.52}{-0.61}$	-0.62	-0.67			207 Pb(n, $\gamma)^{208}$ Pb	1.00, 1.00	
⁹ Bi	-0.77	0.02		209 Bi(n, $\gamma)^{210}$ Bi		10(11, 7) 10	1.00, 1.00	
	$\frac{-0.77}{0.58}$	0.92		$D_1(n, \gamma)$	208 Pb(n, $\gamma)^{209}$ Pb		1.00, 1.00	

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Table A3. Key reaction rates for the model with double the initial 13 C abundance ('2 × 13 C' case). Key rates in levels 1–3 are shown, along with their correlation factors r_{cor0} , r_{cor1} , and r_{cor2} , respectively. Not all s-process nuclides analysed are listed but only those for which key rates were found. Also shown for each rate are the ground-state contributions of the (n,γ) reaction to the stellar rate and uncertainty factors of the β-decay rate at two plasma temperatures, respectively.

Nuclide	$r_{\rm cor,0}$	$r_{\text{cor},1}$	$r_{\rm cor,2}$	Key rate Level 1	Key rate Level 2	Key rate Level 3	X_0 (8, 30 keV)	β -decay
ⁱ⁹ Ga	-0.42	-0.43	-0.92			⁶⁹ Ga(n, γ) ⁷⁰ Ga	1.00, 1.00	
¹ Ga	-0.57	-0.58	-0.96			71 Ga(n, γ) 72 Ga	1.00, 1.00	
⁰ Ge	-0.53	-0.55	-0.95			70 Ge(n, γ) 71 Ge	1.00, 1.00	
² Ge	-0.89			72 Ge(n, γ) 73 Ge		· · · · ·	1.00, 1.00	
	-0.19	-0.69			56 Fe(n, γ) 57 Fe		1.00, 1.00	
	-0.17	-0.68			64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁴ Ge	-0.76			74 Ge(n, γ) 75 Ge	(, , ,		1.00, 1.00	
	-0.40	-0.68		(,,,,	56 Fe(n, γ) 57 Fe		1.00, 1.00	
	-0.41	-0.68			64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁵ As	-0.41	$\frac{-0.46}{}$	-0.91			75 As(n, γ) 76 As	1.00, 1.00	
⁶ Se	-0.46	-0.49	-0.93			76 Se(n, γ) 77 Se	1.00, 1.00	
⁸ Se	-0.87			78 Se(n, γ) 79 Se		(,,,	1.00, 1.00	
50	$\frac{-0.07}{-0.27}$	-0.67		56(11, 7) 56	56 Fe(n, γ) 57 Fe		1.00, 1.00	
	-0.29	$\frac{-0.69}{-0.69}$			64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁰ Se	-0.67			80 Se(n, γ) 81 Se	111(11, 7) 111		1.00, 1.00	
50	$\frac{0.67}{-0.46}$	-0.67		Se(n, y) Se	56 Fe(n, γ) 57 Fe		1.00, 1.00	
	-0.47	$\frac{-0.67}{-0.69}$			64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁹ Br	-0.90			79 Se(n, γ) 80 Se	111(11, 7) 111		1.00, 1.00	
Di	$\frac{-0.50}{-0.19}$	-0.67		σc(n, γ) σc	56 Fe(n, γ) 57 Fe		1.00, 1.00	
	-0.19	$\frac{-0.67}{-0.68}$			64 Ni(n, γ) 65 Ni		1.00, 1.00	
³¹ Br	-0.19 -0.61	$\frac{-0.66}{-0.66}$			64 Ni(n, γ) 65 Ni		1.00, 1.00	
DI	-0.01 -0.26	$\frac{-0.00}{-0.28}$	0.75		Μ(Π, γ) Μ	81 Br(n, $\gamma)^{82}$ Br	1.00, 1.00	
⁰ Kr	-0.26 -0.86	-0.28	-0.75	79 Se(n, γ) 80 Se		$\mathbf{D}\mathbf{I}(\mathbf{II}, \gamma) \mathbf{D}\mathbf{I}$	1.00, 1.00	
Kı	$\frac{-0.86}{0.24}$	0.64	0.84	3c(π, γ) 3c		79 Se(β^{-}) 79 Br	1.00, 1.00	1.30, 1.49
² Kr	-0.64	-0.68	0.84		82 Kr(n, γ) 83 Kr	SC(p) BI	1.00, 1.00	1.30, 1.49
⁴ Kr		_0.08		84 Kr(n, γ) 85 Kr	KI(II, γ) KI			
. VI	$\frac{-0.80}{0.36}$	0.66		$KI(II, \gamma)^{aa}KI$	56 Fe(n, γ) 57 Fe		1.00, 1.00	
	-0.36	$\frac{-0.66}{0.60}$			64 Ni(n, γ) 65 Ni		1.00, 1.00	
6.77	-0.37	-0.69		8517 ()8617	$^{64}Ni(n, \gamma)^{65}Ni$		1.00, 1.00	
⁸⁶ Kr	0.85	0.04		85 Kr(n, γ) 86 Kr	85 rr (a _) 85 m t		1.00, 1.00	4 20 4 20
	-0.41	$\frac{-0.84}{0.52}$	1.00		85 Kr $(\beta^{-})^{85}$ Rb	8617 / 8717	1.00 1.00	1.30, 1.30
.5 m.s	-0.27	-0.52	-1.00		642.11	86 Kr(n, γ) 87 Kr	1.00, 1.00	
³⁵ Rb	-0.60	$\frac{-0.65}{0.000}$			64 Ni(n, γ) 65 Ni	9596	1.00, 1.00	
7	-0.32	-0.36	-0.82	95		85 Rb(n, γ) 86 Rb	1.00, 1.00	
³⁷ Rb	0.87			85 Kr(n, γ) 86 Kr	0505		1.00, 1.00	
	-0.41	$\frac{-0.89}{0.000}$			$^{85}{ m Kr}(eta^-)^{85}{ m Rb}$	9799		1.30, 1.30
06	-0.18	-0.39	$\frac{-0.92}{}$			87 Rb(n, γ) 88 Rb	1.00, 1.00	
⁸⁶ Sr	-0.54	-0.58	-0.94			86 Sr(n, $\gamma)^{87}$ Sr	1.00, 1.00	
⁸⁷ Sr	-0.46	-0.53	-0.91	00 00		87 Sr(n, γ) 88 Sr	1.00, 1.00	
⁸⁸ Sr	-0.66			88 Sr(n, γ) 89 Sr	(1 (5		1.00, 1.00	
10	-0.41	-0.66		00	64 Ni(n, γ) 65 Ni		1.00, 1.00	
⁸⁹ Y	-0.81			89 Y(n, $\gamma)^{90}$ Y			1.00, 1.00	
⁹⁰ Zr	-0.92			90 Zr(n, $\gamma)^{91}$ Zr			1.00, 1.00	
⁰² Zr	-0.94			92 Zr(n, γ) 93 Zr			1.00, 1.00	
⁹⁴ Zr	-0.89			94 Zr(n, γ) 95 Zr			1.00, 1.00	
⁰³ Nb	-0.97			93 Zr(n, γ) 94 Zr			1.00, 1.00	
⁵ Mo	-0.88			95 Mo(n, γ) 96 Mo			1.00, 1.00	
⁶ Mo	-0.96			96 Mo(n, $\gamma)^{97}$ Mo			1.00, 1.00	
⁷ Mo	-0.89			97 Mo(n, γ) 98 Mo			1.00, 1.00	
⁸ Mo	-0.95			98 Mo(n, γ) 99 Mo			1.00, 1.00	
⁹ Ru	-0.92			99 Tc(n, γ) 100 Tc			1.00, 1.00	
.00Ru	-0.94			100 Ru(n, γ) 101 Ru			1.00, 1.00	
	0.10	0.48	0.65			86 Kr(n, γ) 87 Kr	1.00, 1.00	
⁰² Ru	-0.88			102 Ru(n, γ) 103 Ru			1.00, 1.00	
	0.15	0.47	0.65			86 Kr(n, γ) 87 Kr	1.00, 1.00	
¹⁰³ Rh	-0.95			103 Rh(n, γ) 104 Rh			0.95, 0.80	
	0.09	0.47	0.66	() /)		86 Kr(n, γ) 87 Kr	1.00, 1.00	
			2.00	104 Pd(n, γ) 105 Pd		(, / /		
¹⁰⁴ Pd	-0.97			104 Pa(n, ν) 103 Pa			1.00, 1.00	

Table A3 - continued

Nuclide	$r_{\rm cor,0}$	$r_{\rm cor,1}$	$r_{\rm cor,2}$	Key rate Level 1	Key rate Level 2	Key rate Level 3	X_0 (8, 30 keV)	β -decay
⁰⁶ Pd	-0.97			$^{106}\text{Pd}(n, \gamma)^{107}\text{Pd}$			1.00, 1.00	
	0.07	0.65			85 Kr(β^{-}) 85 Rb			1.30, 1.30
	0.05	0.46	0.67			86 Kr(n, γ) 87 Kr	1.00, 1.00	
⁰⁸ Pd	-0.97			$^{108}\text{Pd}(n, \gamma)^{109}\text{Pd}$			1.00, 1.00	
	0.10	0.65			85 Kr(β^{-}) 85 Rb			1.30, 1.30
	0.05	0.45	0.67			86 Kr(n, γ) 87 Kr	1.00, 1.00	
⁰⁷ Ag	-0.82			$^{107}\text{Pd}(n, \gamma)^{108}\text{Pd}$			1.00, 1.00	
	0.19	0.65			$^{85}{\rm Kr}(\beta^-)^{85}{\rm Rb}$	0.5		1.30, 1.30
	0.14	0.46	0.67			86 Kr(n, γ) 87 Kr	1.00, 1.00	
⁰⁹ Ag	-0.81			109 Ag(n, $\gamma)^{110}$ Ag			1.00, 1.00	
	0.19	0.65			85 Kr(β^{-}) 85 Rb	0.5		1.30, 1.30
10	0.17	0.45	0.67	05		86 Kr(n, γ) 87 Kr	1.00, 1.00	
¹⁰ Cd	-0.67			85 Kr(n, γ) 86 Kr	110		1.00, 1.00	
	-0.42	-0.71			$^{110}\text{Cd}(n, \gamma)^{111}\text{Cd}$	0.6	1.00, 1.00	
10	0.23	0.31	0.67	05		86 Kr(n, γ) 87 Kr	1.00, 1.00	
¹² Cd	-0.69			85 Kr(n, γ) 86 Kr	112		1.00, 1.00	
	-0.41	-0.68			$^{112}\text{Cd}(n, \gamma)^{113}\text{Cd}$	06 07	1.00, 1.00	
1.4	0.23	0.33	0.69	05 06		86 Kr(n, γ) 87 Kr	1.00, 1.00	
¹⁴ Cd	-0.70			85 Kr(n, γ) 86 Kr		114 115	1.00, 1.00	
15-	-0.36	-0.63	-0.81	115 116-		$^{114}\text{Cd}(n, \gamma)^{115}\text{Cd}$	1.00, 1.00	
¹⁵ In	$\frac{-0.97}{}$			115 In(n, γ) 116 In	0505		1.00, 1.00	
	0.07	0.65			85 Kr(β^{-}) 85 Rb	96		1.30, 1.30
16	0.06	0.42	<u>0.70</u>	05		86 Kr(n, γ) 87 Kr	1.00, 1.00	
¹⁶ Sn	$\frac{-0.66}{0.56}$			85 Kr(n, γ) 86 Kr	116		1.00, 1.00	
	-0.50	$\frac{-0.77}{0.000}$			116 Sn(n, γ) 117 Sn	96 , 97	1.00, 1.00	
10 a	0.19	0.25	0.71		119 0 110 0	86 Kr(n, γ) 87 Kr	1.00, 1.00	
¹⁸ Sn	-0.55	$\frac{-0.81}{0.10}$	0.71		118 Sn(n, γ) 119 Sn	86++ ()87++	1.00, 1.00	
20 a	0.18	0.19	0.74	85*** \ 86**		86 Kr(n, γ) 87 Kr	1.00, 1.00	
¹²⁰ Sn	$\frac{-0.65}{0.52}$	0.76		85 Kr(n, γ) 86 Kr	120 Sn(n, γ) 121 Sn		1.00, 1.00	
	-0.52	$\frac{-0.76}{0.22}$	0.70		120 Sn(n, γ) 121 Sn	86 Kr(n, γ) 87 Kr	1.00, 1.00	
¹²¹ Sb	0.17	0.22	<u>0.79</u>	121 Sb $(n, \gamma)^{122}$ Sb		66 Kr(n, γ) 67 Kr	1.00, 1.00	
21 Sb	$\frac{-0.89}{0.00}$	0.22	0.70	$^{121}Sb(n, \gamma)^{122}Sb$		86 Kr(n, γ) 87 Kr	0.98, 0.93	
²² Te	0.09	0.32	<u>0.79</u>	85 Kr(n, γ) 86 Kr		$^{\circ\circ}$ Kr(n, γ) $^{\circ\circ}$ Kr	1.00, 1.00	
1e	$\frac{-0.71}{-0.34}$	-0.54	0.80	$Kr(n, \gamma)^{**}Kr$		$^{122}\text{Te}(n, \gamma)^{123}\text{Te}$	1.00, 1.00	
²³ Te		-0.34	-0.80	85 Kr(n, γ) 86 Kr		$r=1e(n, \gamma)$	1.00, 1.00	
16	$\frac{-0.71}{0.35}$	0.54	0.80	$KI(II, \gamma)$		$^{123}\text{Te}(n, \gamma)^{124}\text{Te}$	1.00, 1.00	
¹²⁴ Te		0.34	0.80	85 Kr(n, γ) 86 Kr		$\operatorname{Ie}(\Pi, \gamma)$ Ie	1.00, 1.00 1.00, 1.00	
16	$\frac{-0.68}{0.45}$	0.60		$KI(II, \gamma)$ KI	$^{124}\text{Te}(n, \gamma)^{125}\text{Te}$			
	-0.45 0.17	$\frac{-0.69}{0.22}$	0.91		$Ie(II, \gamma)$	86 Kr(n, γ) 87 Kr	1.00, 1.00 1.00, 1.00	
²⁶ Te	-0.60	<u>-0.80</u>	<u>0.81</u>		$^{126}\text{Te}(n, \gamma)^{127}\text{Te}$	KI(II, γ) KI	1.00, 1.00	
10	0.14	0.17	0.83		$Ie(II, \gamma)$ Ie	86 Kr(n, γ) 87 Kr	1.00, 1.00	
²⁷ I	<u>-0.87</u>	0.17	0.03	$^{127}I(n, \gamma)^{128}I$		KI(II, γ) KI	1.00, 0.99	
1	$\frac{-0.87}{0.09}$	0.28	0.83	$I(\Pi, \gamma) = I$		86 Kr(n, γ) 87 Kr	1.00, 0.99	
²⁸ Xe	0.57	0.72	0.03		$^{128}I(\beta^-)^{128}Xe$	Ki(ii, y) Ki	1.00, 1.00	1.64, 5.42
AC	-0.22	-0.27	-0.69		$I(p^{-})$ Ac	$^{128}I(\beta^+)^{128}Te$		1.04, 3.42
³⁰ Xe	-0.22 -0.67	-0.27	_0.07	85 Kr(n, γ) 86 Kr		$I(p^{-})$	1.00, 1.00	
710	$\frac{0.07}{-0.44}$	-0.67		M(n, y) M	130 Xe(n, γ) 131 Xe		1.00, 1.00	
	0.16	0.19	0.86		$\mathcal{H}_{\mathbf{C}}(\mathbf{n},\gamma)$	86 Kr(n, γ) 87 Kr	1.00, 1.00	
³² Xe	<u>-0.94</u>	0.17	0.00	132 Xe(n, γ) 133 Xe		Ki(ii, y) Ki	1.00, 1.00	
210	$\frac{0.54}{0.05}$	0.23	0.87	$\mathcal{H}\mathbf{c}(\mathbf{n},\gamma)$		86 Kr(n, γ) 87 Kr	1.00, 1.00	
³³ Cs	-0.80	0.23	0.07	133 Cs(n, γ) 134 Cs		III(II,) III	1.00, 1.00	
0.5	0.12	0.23	0.87	C5(n, 7) C5		86 Kr(n, γ) 87 Kr	1.00, 1.00	
³⁴ Ba	-0.75	0.23	0.07	134 Ba(n, γ) 135 Ba		m(n, y) m	1.00, 1.00	
	0.10	0.22	0.73	24(11, 7) 154		86 Kr(n, γ) 87 Kr	1.00, 1.00	
³⁶ Ba	-0.78		2.70	136 Ba(n, γ) 137 Ba		(, /)	1.00, 1.00	
	0.10	0.20	0.87			86 Kr(n, γ) 87 Kr	1.00, 1.00	
³⁷ Ba	-0.72	3.23	3.07	137 Ba(n, γ) 138 Ba		(, / / 151	1.00, 1.00	
	$\frac{0.72}{0.12}$	0.19	0.87	(, / /		86 Kr(n, γ) 87 Kr	1.00, 1.00	
³⁸ Ba	-0.87	3.27	3.07	138 Ba(n, γ) 139 Ba		(, / / 151	1.00, 1.00	
	0.23	0.65		(, / /	64 Ni(n, γ) 65 Ni		1.00, 1.00	
³⁹ La	<u>-0.96</u>	5.05		139 La(n, γ) 140 La	(11, / / 141		1.00, 1.00	
	0.70			Lu(11, γ) Lu				
La	0.11	0.65			64 Ni(n, γ) 65 Ni		1.00, 1.00	

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Table A3 - continued

Nuclide	$r_{\rm cor,0}$	$r_{\text{cor},1}$	$r_{\rm cor,2}$	Key rate Level 1	Key rate Level 2	Key rate Level 3	X_0 (8, 30 keV)	β -decay
⁴² Nd	-0.73			142 Nd(n, γ) 143 Nd			1.00, 1.00	
¹⁴ Nd	-0.66			144 Nd(n, γ) 145 Nd			1.00, 1.00	
⁶ Nd	$\frac{-0.06}{-0.26}$	-0.42	-0.69	114(11, 7)		146 Nd(n, γ) 147 Nd	1.00, 1.00	
⁷ Sm	-0.20 -0.31	-0.42 -0.50	$\frac{-0.05}{-0.76}$			147 Sm(n, γ) 148 Sm	1.00, 1.00	
⁸ Sm	-0.31 -0.29					148 Sm(n, γ) 149 Sm		
⁰ Sm		-0.48	-0.73	138 Ba(n, γ) 139 Ba		$\operatorname{Sm}(n, \gamma)$ Sm	1.00, 1.00	
Sm	0.66						1.00, 1.00	
Eu	-0.93			151 Eu(n, γ) 152 Eu		152	0.89, 0.79	
³ Eu	-0.32	-0.57	-0.80			153 Eu(n, γ) 154 Eu	1.00, 1.00	
² Gd	0.80			151 Sm $(\beta^{-})^{151}$ Eu				3.60, 5.42
	-0.16	-0.74			151 Sm(n, γ) 152 Sm		0.80, 0.76	
⁶ Gd	-0.51	-0.73			156 Gd(n, γ) 157 Gd		1.00, 0.99	
⁸ Gd	-0.65			158 Gd(n, γ) 159 Gd			1.00, 0.98	
⁹ Tb	-0.97			159 Tb(n, γ) 160 Tb			1.00, 0.98	
⁰ Dy	$\frac{-0.65}{-0.65}$			160 Dy(n, γ) 161 Dy			1.00, 0.99	
² Dy	$\frac{0.69}{-0.69}$			162 Dy(n, γ) 163 Dy			1.00, 0.98	
⁴ Dy				164 Dy(n, γ) 165 Dy				
	$\frac{-0.80}{0.05}$						1.00, 0.97	
⁵ Ho	$\frac{-0.95}{0.00}$			$^{165}\text{Ho}(n, \gamma)^{166}\text{Ho}$			1.00, 1.00	
⁶ Er	-0.97			166 Er(n, $\gamma)^{167}$ Er			1.00, 0.98	
⁷ Er	-0.97			167 Er(n, γ) 168 Er			1.00, 1.00	
⁸ Er	-0.98			168 Er(n, $\gamma)^{169}$ Er			1.00, 0.98	
⁹ Tm	-0.97			169 Tm(n, γ) 170 Tm			0.51, 0.42	
0 Yb	-0.64	-0.84			170 Yb(n, γ) 171 Yb		1.00, 0.99	
² Yb	-0.71			172 Yb(n, γ) 173 Yb			1.00, 0.98	
⁴ Yb	-0.72			174 Yb(n, γ) 175 Yb			1.00, 0.98	
⁵ Lu	0.70			138 Ba(n, γ) 139 Ba			1.00, 1.00	
⁶ Lu	0.66			138 Ba(n, γ) 139 Ba			1.00, 1.00	
⁶ Hf				$^{176}\text{Lu}(\beta^-)^{176}\text{Hf}$			1.00, 1.00	1 20 1 20
П	0.90	0.40	0.60	Lu(p) In		176 Hf(n, γ) 177 Hf	1.00.000	1.30, 1.33
9	-0.11	-0.48	-0.69		178 170	170 HI(n, γ) 177 HI	1.00, 0.99	
⁸ Hf	-0.48	-0.72			178 Hf(n, γ) 179 Hf		1.00, 0.99	
⁰ Hf	-0.53	-0.78		404	180 Hf(n, γ) 181 Hf		1.00, 0.99	
¹ Ta	-0.98			181 Ta(n, γ) 182 Ta			0.61, 0.55	
^{2}W	-0.77			182 W(n, γ) 183 W			1.00, 1.00	
^{3}W	-0.91			183 W(n, γ) 184 W			0.99, 0.93	
^{4}W	-0.58	-0.83			184 W(n, γ) 185 W		1.00, 1.00	
⁵ Re	-0.80			185 Re(n, γ) 186 Re			1.00, 1.00	
⁶ Os	$\frac{-0.74}{-0.74}$			186 Os(n, γ) 187 Os			1.00, 1.00	
O ₃	0.34	0.68		$Os(n, \gamma)$ Os	186 Re $(\beta^{-})^{186}$ Os		1.00, 1.00	1.30, 3.59
			0.77		Ke(p) Os	186 Re $(\beta^+)^{186}$ W		1.30, 3.35
7.0	-0.21	-0.43	-0.77	1870 ()1880		100 Re(β 1)100 W	0.57.0.46	
⁷ Os	-0.97			187 Os(n, γ) 188 Os	106 106		0.57, 0.46	
	0.07	0.67			186 Re $(\beta^{-})^{186}$ Os	406		1.30, 3.59
	-0.05	-0.43	-0.76			$^{186}\text{Re}(\beta^+)^{186}\text{W}$		
⁸ Os	-0.84			188 Os(n, γ) 189 Os			1.00, 1.00	
0 Os	-0.78			190 Os(n, γ) 191 Os			1.00, 1.00	
¹ Ir	-0.62	-0.86		• • •	191 Ir(n, γ) 192 Ir		1.00, 1.00	
³ Ir	-0.90			193 Ir(n, γ) 194 Ir	· · • /		1.00, 0.99	
	$\frac{0.30}{-0.31}$	-0.91		/ / 	193 Pt(n, γ) 194 Pt		0.25, 0.21	
² Pt	-0.96			192 Pt(n, γ) 193 Pt	Ι ((11, γ) Ι (1.00, 1.00	
11	0.04	0.74		1 t(11, γ) 1 t	$^{192}\text{Ir}(\beta^-)^{192}\text{Pt}$		1.00, 1.00	1 21 6 24
4p.		<u>0.74</u>		104p./ \105p.	$\operatorname{Ir}(p)$) Pt		1.00 1.00	1.31, 6.36
⁴ Pt	$\frac{-0.94}{0.001}$			194 Pt(n, γ) 195 Pt	102 104-		1.00, 1.00	
6-	-0.04	-0.73		106- 107	193 Pt(n, γ) 194 Pt		0.25, 0.21	
⁶ Pt	-0.96			196 Pt(n, γ) 197 Pt			1.00, 1.00	
⁷ Au	0.73			138 Ba(n, γ) 139 Ba			1.00, 1.00	
⁸ Hg	-0.96			198 Hg(n, γ) 199 Hg			1.00, 1.00	
0 Hg	-0.97			200 Hg(n, γ) 201 Hg			1.00, 1.00	
² Hg	$\frac{-0.77}{-0.77}$			202 Hg(n, γ) 203 Hg			1.00, 1.00	
³ Tl	$\frac{0.77}{-0.94}$			$^{203}\text{Tl}(n, \gamma)^{204}\text{Tl}$			1.00, 1.00	
⁵ Tl	$\frac{-0.94}{-0.94}$			$^{205}\text{Pb}(n, \gamma)^{206}\text{Pb}$				
⁴ Pb							0.83, 0.82	
	$\frac{-0.84}{0.55}$			204 Pb(n, γ) 205 Pb	206		1.00, 1.00	
⁶ Pb	-0.59	-0.88			206 Pb(n, $\gamma)^{207}$ Pb		1.00, 1.00	
⁷ Pb	-0.64	-0.81			207 Pb(n, γ) 208 Pb		1.00, 1.00	
⁹ Bi	0.68			208 Pb(n, γ) 209 Pb			1.00, 1.00	
	-0.36	-0.57	-0.95	•		209 Bi(n, $\gamma)^{210}$ Bi	1.00, 1.00	

Table A4. The key reaction rates for the TP model. Key rates in levels 1-3 are shown, along with their correlation factors r_{cor0} , r_{cor1} , and r_{cor2} , respectively. Not all s-process nuclides analysed are listed but only those for which key rates were found. Also shown for each rate are the ground state contributions X_0 to the stellar rate of the (n,γ) reaction and uncertainty factors of the β -decay rate at two plasma temperatures, respectively.

Nuclide	$r_{\rm cor,0}$	$r_{\rm cor,1}$	$r_{\rm cor,2}$	Key rate Level 1	Key rate Level 2	Key rate Level 3	X_0 (8, 30 keV)	β -decay
⁷⁰ Ge	-0.83			70 Ge(n, γ) 71 Ge			1.00, 1.00	
	0.41	0.73		(, , ,	68 Zn(n, γ) 69 Zn		1.00, 1.00	
	0.36	0.67			69 Ga(n, γ) 70 Ga		1.00, 1.00	
	-0.04	-0.11	<u>-0.94</u>		Gu(ii, y) Gu	70 Ga(n, γ) 71 Ga	1.00, 1.00	
Se	0.76	0.11		74 Ge(n, γ) 75 Ge		Gu(ii, y) Gu	1.00, 1.00	
SC	-0.59	0.00		GC(II, y) GC	76 Se(n, γ) 77 Se		1.00, 1.00	
		$\frac{-0.90}{0.37}$	0.04		Se(II, γ) Se	75 As(n, γ) 76 As		
³² Se	0.27	0.57	0.84	81 g ()82 g		$As(\Pi, \gamma)$ As	1.00, 1.00	
Se	0.88	0.02		81 Se(n, γ) 82 Se	82 0 4 83 0		1.00, 1.00	
	-0.30	$\frac{-0.83}{0.000}$			82 Se(n, γ) 83 Se	91 91 -	1.00, 1.00	
	-0.27	-0.46	-0.85	00 00		81 Se $(\beta^{-})^{81}$ Br		1.30, 2.1
)Kr	0.66			80 Br(β^{-}) 80 Kr				1.31, 4.7
_	-0.47	-0.66			$^{80}{ m Kr}({ m n},\gamma)^{81}{ m Kr}$		1.00, 1.00	
⁵ Sr	-0.92			86 Sr(n, γ) 87 Sr			1.00, 1.00	
	-0.27	-0.71			86 Rb(n, $\gamma)^{87}$ Rb		1.00, 1.00	
	0.15	0.39	0.89			85 Rb(n, $\gamma)^{86}$ Rb	1.00, 1.00	
⁷ Sr	0.65			86 Sr(n, γ) 87 Sr			1.00, 1.00	
	-0.75			87 Sr(n, γ) 88 Sr			1.00, 1.00	
	0.04	0.44	0.76	SI(II,) SI		85 Rb(n, γ) 86 Rb	1.00, 1.00	
5Zr	-0.74	0.77	0.70	95 Zr(β^{-}) 95 Nb		Ro(n, y) Ro	1.00, 1.00	
ZI	$\frac{-0.74}{0.46}$	0.00		$\Sigma I(p^{-})$ No	95 Zr(n, γ) 96 Zr		1.00 1.00	
		0.98	0.05		$\Sigma \Gamma(n, \gamma) \Sigma \Gamma$	947 ()957	1.00, 1.00	
1	0.06	0.13	0.95	04		94 Zr(n, γ) 95 Zr	1.00, 1.00	
⁴ Mo	-0.80			94 Mo(n, γ) 95 Mo	04 05		1.00, 1.00	
	-0.43	-0.71			94 Nb(n, γ) 95 Nb	0.4	0.99, 0.97	
_	0.33	0.56	0.81			94 Nb(β^{-}) 94 Mo		1.35, 3.22
⁶ Mo	-0.66			96 Mo(n, γ) 97 Mo			1.00, 1.00	
00 Mo	0.85			99 Mo(n, γ) 100 Mo			1.00, 1.00	
	-0.42	-0.82			$^{99}\text{Mo}(\beta^{-})^{99}\text{Tc}$			1.30, 2.1
	-0.14	$\frac{-0.82}{-0.32}$	-1.00			100 Mo(n, γ) 101 Mo	1.00, 1.00	
⁰⁰ Ru	-0.79			100 Ru(n, γ) 101 Ru			1.00, 1.00	
	0.57	0.95			98 Mo(n, γ) 99 Mo		1.00, 1.00	
	0.18	$\frac{0.52}{0.29}$	0.91		1110(11, 7) 1110	$^{99}\text{Tc}(n, \gamma)^{100}\text{Tc}$	1.00, 1.00	
⁰⁴ Ru	0.65	0.27	0.71	103 Ru(n, γ) 104 Ru		10(n, y) 10	0.45, 0.41	
ιχu	-0.49	-0.67		Ru(π, γ) Ru	103 Ru $(\beta^{-})^{103}$ Rh		0.43, 0.41	5.76, 6.3
	-0.49 -0.06	$\frac{-0.07}{-0.06}$	0.00		$\mathbf{Ku}(p^-)$ Kii	104 Ru(n, γ) 105 Ru	1.00, 1.00	3.70, 0.3
⁰⁴ Pd		-0.00	-0.98	104 Pd(n, γ) 105 Pd		Ku(II, γ) · · · Ku		
· Pa	$\frac{-0.95}{0.20}$	0.60		$Pa(n, \gamma)^{100}$ Pa	1025 ()1035		1.00, 1.00	
	0.20	0.69			102 Ru(n, γ) 103 Ru		1.00, 1.00	
10	0.20	0.66		100 110	103 Rh(n, $\gamma)^{104}$ Rh		0.95, 0.80	
¹⁰ Pd	0.86			109 Pd(n, γ) 110 Pd			1.00, 1.00	
¹⁰ Cd	0.87			108 Pd(n, γ) 109 Pd			1.00, 1.00	
	0.31	0.75			106 Pd(n, γ) 107 Pd		1.00, 1.00	
	0.20	0.47	0.72			109 Ag(n, γ) 110 Ag	1.00, 1.00	
¹¹⁶ Cd	0.96			$^{115}\text{Cd}(n, \gamma)^{116}\text{Cd}$			1.00, 1.00	
	-0.26	-0.96			$^{115}\text{Cd}(\beta^{-})^{115}\text{In}$			1.30, 1.44
¹⁴ Sn	0.66			113 Sn(n, γ) 114 Sn	٧ /		1.00, 0.99	,
~	0.55	0.77		(, / / 511	112 Sn(n, γ) 113 Sn		1.00, 1.00	
¹⁵ Sn	0.67	5.77		113 Sn(n, γ) 114 Sn	S(II, 7) SII		1.00, 0.99	
	-0.45	-0.59	0.66	σn(n, γ) σn		115 Sn(n, γ) 116 Sn	1.00, 0.99	
		-0.39	-0.66	115 In(n, γ) 116 In		Su(II, Y) SII		
Su	0.81	0.02		$m(n, \gamma)^{-1}$ In	1160 ()1170		1.00, 1.00	
24 ~	-0.27	$\frac{-0.82}{0.42}$	0		116 Sn(n, γ) 117 Sn	116	1.00, 1.00	
	-0.15	-0.42	-0.89	102 104		116 In(n, γ) 117 In	1.00, 1.00	
²⁴ Sn	0.96			123 Sn(n, γ) 124 Sn			0.98, 0.96	
²² Te	<u>0.74</u>			121 Sb(n, γ) 122 Sb	100		0.98, 0.93	
²³ Te	-0.60	-0.78			$^{123}\text{Te}(n, \gamma)^{124}\text{Te}$		1.00, 1.00	
²⁴ Te	0.87			121 Sb(n, γ) 122 Sb			0.98, 0.93	
	-0.37	-0.71			$^{124}\text{Te}(n, \gamma)^{125}\text{Te}$		1.00, 1.00	
³⁰ Te	-0.78			$^{130}I(\beta^{-})^{130}Xe$				1.31, 4.9
²⁸ Xe	0.75			$^{128}I(\beta^{-})^{128}Xe$				1.64, 5.4
AC	0.31	0.66		-(1) / 110	$^{127}I(n, \gamma)^{128}I$		1.00, 0.99	1.01, 0.7.
110		0.00			1(11, <i>y</i>) 1			
				129 Y e(n 1130 V 2			0.00 0.00	
³⁰ Xe	0.83 0.32	0.67		129 Xe(n, γ) 130 Xe	$^{127}I(n, \gamma)^{128}I$		0.98, 0.90 1.00, 0.99	

Table A4 - continued

Nuclide	$r_{\rm cor,0}$	$r_{\rm cor,1}$	$r_{\rm cor,2}$	Key rate Level 1	Key rate Level 2	Key rate Level 3	X_0 (8, 30 keV)	β -decay
.34Xe	-0.68			$^{134}\text{Cs}(\beta^-)^{134}\text{Ba}$				3.24, 5.5
	0.39	0.83			133 Xe(n, γ) 134 Xe		1.00, 1.00	
	-0.10	-0.20	-0.70		(, /)	133 Xe(β^{-}) 133 Cs	,	1.30, 1.3
	0.08	0.15	0.66			131 Xe(n, γ) 132 Xe	1.00, 1.00	
Xe	-0.66	0.10	0.00	134 Cs $(\beta^{-})^{134}$ Ba		110(11, 7) 110	1.00, 1.00	3.24, 5.5
710	0.39	0.86		C5(p') Bu	134 Cs(n, γ) 135 Cs		0.78, 0.68	3.21, 3.0
	-0.19	-0.40	-0.90		C5(II, 7) C5	$^{136}\text{Cs}(\beta^{-})^{136}\text{Ba}$	0.70, 0.00	
³⁴ Ba	0.64		-0.50		132 Xe(n, γ) 133 Xe	Cs(p) Ba	1.00, 1.00	
⁶ Ва		0.72	0.77		$Ae(II, \gamma)$	134 Ba(n, γ) 135 Ba		
	-0.38	-0.40	-0.77	136 Ba(n, γ) 137 Ba		13 Ba(n, γ) 133 Ba	1.00, 1.00	
ъа	$\frac{-0.82}{0.37}$	0.64	0.71	130 Ba(n, γ) 137 Ba		134p ()135p	1.00, 1.00	
	0.37	0.64	0.71	120-		134 Ba(n, γ) 135 Ba	1.00, 1.00	
³ La	-0.94			138 La(n, γ) 139 La	127 120		1.00, 1.00	
	0.14	0.66			137 La(n, γ) 138 La	106 107	0.87, 0.80	
	0.07	0.32	0.82			136 Ce(n, γ) 137 Ce	1.00, 1.00	
Ce	-0.69			$^{141}\text{Ce}(\beta^-)^{141}\text{Pr}$				
	0.40	0.93			141 Ce(n, γ) 142 Ce		1.00, 1.00	
Nd	-0.68			$^{147}\text{Nd}(\beta^-)^{147}\text{Pm}$				1.30, 3.0
	0.65			147 Nd(n, γ) 148 Nd			1.00, 0.98	
	-0.05	-0.66		, ,	56 Fe(n, γ) 57 Fe		1.00, 1.00	
	-0.02	$\frac{-0.65}{-0.67}$			57 Fe(n, γ) 58 Fe		0.73, 0.59	
Sm	0.48	0.65			$^{148}\text{Pm}(\beta^{-})^{148}\text{Sm}$		0.75, 0.57	1.30, 2.7
JIII	0.35	0.70			147 Pm(n, γ) 148 Pm		1.00, 1.00	1.50, 2.
⁰ Sm	0.66	0.70		148 Pm(n, γ) 149 Pm	$I III(II, \gamma) = I III$		1.00, 1.00	
SIII		0.72		$PIII(II, \gamma)$	147 Pm(n, γ) 148 Pm			
	0.47	0.73	0.01		$Pm(n, \gamma)$ Pm	149 Sm(n, γ) 150 Sm	1.00, 1.00	
2 ~	0.07	0.13	0.91	152		$Sm(n, \gamma)^{130}Sm$	0.97, 0.93	
Sm	-0.76			152 Sm(n, γ) 153 Sm		140 150	1.00, 1.00	
	0.13	0.31	0.95			149 Sm(n, γ) 150 Sm	0.97, 0.93	
² Gd	0.93			151 Sm $(\beta^{-})^{151}$ Eu				3.60, 5.4
	-0.31	-0.89			151 Sm(n, γ) 152 Sm		0.80, 0.76	
⁴ Gd	-0.75			154 Gd(n, γ) 155 Gd			1.00, 1.00	
⁰ Gd	0.81			159 Gd(n, γ) 160 Gd			1.00, 0.97	
0 Dy	-0.85			160 Dy(n, γ) 161 Dy			1.00, 0.99	
⁰ Er	-0.66			$^{169}\text{Er}(\beta^{-})^{169}\text{Tm}$,	1.30, 4.4
	0.55	0.90		(,)	169 Er(n, γ) 170 Er		1.00, 0.98	,
	0.21	$\frac{0.35}{0.34}$	0.80		21(11, 7) 21	168 Er(n, γ) 169 Er	1.00, 0.98	
⁰ Yb	-0.85	0.51	0.00	170 Tm(n, γ) 171 Tm		Li(ii, /) Li	0.98, 0.91	
	0.90			175 Yb(n, γ) 176 Yb			1.00, 1.00	
⁷⁶ Yb		0.04		1 υ(II, γ) 1 υ	175 Yb $(\beta^{-})^{175}$ Lu		1.00, 1.00	1 20 1 6
	-0.26	$\frac{-0.84}{0.48}$	0.00		Y b(p) Y Lu	176 Yb(n, γ) 177 Yb	1.00.000	1.30, 1.5
76.	-0.15	-0.48	-0.98	174		$\gamma \circ \gamma \circ (n, \gamma) \gamma \gamma \gamma \circ $	1.00, 0.98	
⁷⁶ Lu	0.85			174 Yb(n, γ) 175 Yb	176		1.00, 0.98	
	-0.37	-0.72			176 Lu(β^{-}) 176 Hf			1.30, 1.3
	0.30	0.55	0.83			172 Yb(n, γ) 173 Yb	1.00, 0.98	
6W	-0.83			$^{185}W(\beta^{-})^{185}Re$				1.44, 3.8
	0.31	0.71			185 W(n, γ) 186 W		0.98, 0.95	
Re	-0.54	-0.62	-0.68			186 Re $(\beta^{-})^{186}$ Os		1.30, 3.5
Os	0.72			$^{185}W(\beta^{-})^{185}Re$				1.44, 3.8
⁸⁷ Os	-0.43	-0.67		* .	186 Os(n, γ) 187 Os		1.00, 1.00	
	-0.88			187 Os(n, γ) 188 Os			0.57, 0.46	
	0.14	0.58	0.67	() ()		186 Re $(\beta^{-})^{186}$ Os		1.30, 3.5
⁹² Os	0.85	0.00	0.07	191 Os(n, γ) 192 Os		110(p) 05	1.00, 1.00	1,00,01
	-0.44	-0.82		ου(11, γ) συ	191 Os $(\beta^{-})^{191}$ Ir		1.00, 1.00	1.30, 1.
	-0.44 -0.17	$\frac{-0.82}{-0.35}$	_0.71		$Oo(p^{-})$ II	192 Os(n, γ) 193 Os	1.00, 1.00	1.50, 1.
⁹² Pt		-0.33	-0.71	192 Pt(n, γ) 193 Pt		$Os(II, \gamma) = Os$		
I l	$\frac{-0.69}{0.56}$	0.01		$F((11, \gamma)^{-1})$	192 Ir(n, γ) 193 Ir		1.00, 1.00	
	-0.56	$\frac{-0.81}{0.50}$	0.00		$r(n, \gamma)^{1/3}$ Ir	1921 (2=)1925	0.64, 0.51	101 (
⁹⁵ Pt	0.33	0.50	0.90	105 p. (106 –		$^{192}\text{Ir}(\beta^-)^{192}\text{Pt}$	4.00	1.31, 6.3
	-0.91			195 Pt(n, γ) 196 Pt	104		1.00, 1.00	
	0.22	0.88		408	194 Pt(n, γ) 195 Pt		1.00, 1.00	
Pt	0.91			197 Pt(n, γ) 198 Pt			0.99, 0.94	
	-0.27	-0.71			197 Pt $(\beta^{-})^{197}$ Au			1.31, 4.9
	-0.06	-0.20	-1.00			198 Pt(n, γ) 199 Pt	1.00, 1.00	
³ Hg	-0.70			198 Hg(n, γ) 199 Hg		· · • • /	1.00, 1.00	
C	0.49	0.78		5.77	196 Pt(n, γ) 197 Pt		1.00, 1.00	
			-0.76		, / /	198 Au(n, γ) 199 Au	1.00, 1.00	

Table A4 - continued

Nuclide	$r_{\rm cor,0}$	$r_{\rm cor,1}$	$r_{\rm cor,2}$	Key rate Level 1	Key rate Level 2	Key rate Level 3	X_0 (8, 30 keV)	β -decay
²⁰⁴ Pb	0.76			203 Tl(n, γ) 204 Tl			1.00, 1.00	
	-0.47	-0.74			204 Tl $(n, \gamma)^{205}$ Tl		1.00, 1.00	
	-0.38	-0.59	-0.89			204 Pb(n, γ) 205 Pb	1.00, 1.00	
²⁰⁹ Bi	0.94			208 Pb(n, $\gamma)^{209}$ Pb			1.00, 1.00	
	-0.32	-0.91			209 Bi(n, $\gamma)^{210}$ Bi		1.00, 1.00	

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