Majorana-like Coulomb spectroscopy in the absence of zero bias peaks

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Hybrid semiconductor-superconductor devices hold
great promise for realizing topological quantum
computing with Majorana zero modes [1, 2, 3, 4,
5, 6, 7]. However, multiple claims of Majorana detection, based on either tunneling [8, 9, 10, 11, 12]
or Coulomb spectroscopy [13, 14], remain disputed.
Here we devise an experimental protocol that allows to perform both types of measurements on lows to perform both types of measurements on the same hybrid island by adjusting its chargthe same hybrid island by adjusting its charging energy via tunable junctions to the normal leads. This method reduces ambiguities of Majorana detections by checking the consistency between Coulomb spectroscopy and zero bias peaks in non-blockaded transport. Specifically we observe junction-dependent, even-odd modulated, single-electron Coulomb peaks without concomitant lowbias peaks in tunneling spectroscopy. We provide a theoretical interpretation of the experimental observations in terms of low-energy, longitudinallyconfined, island states rather than overlapping Ma-; jorana modes. Our method highlights the importance of combined measurements on the same device for the identification of topological Majorana

2 \mathbf{Main}

One of the most hunted-for signatures of a Majorana zero mode (MZM) at the edge of a one-dimensional topological superconductor is a resonant zero bias peak (ZBP) in tunneling spectroscopy experiments [15, 16, 17, 7]. For hybrid nanowires (NWs) this was first reported in 2012 [8] with several other works appearing in the following years [9, 10, 11, 12]. However, by now it has become clear that peaks pinned to zero bias cannot be easily distinguished from those of non-topological origin. Unintentional quantum dots (QDs) [18, 19, 20], NW smooth confinement [21, 22, 23, 24, 25, 26, 27, 28] and/or disorder in the semiconductor [29, 30] can give rise to topologically trivial zero energy states that mimic many of the properties of their topological counterparts. An alternative route to detect MZM signatures is Coulomb blockade spectroscopy [13, 14], where the transition from coherent two-electron (2-e) to one-electron (1-e) transport and the exponential length dependence of the 1-e Coulomb peak spacing are associated with the appearance of topological excitations. In contrast to tunneling spectroscopy measurements, the observation of parity transitions in Coulomb blockade appears surprisingly

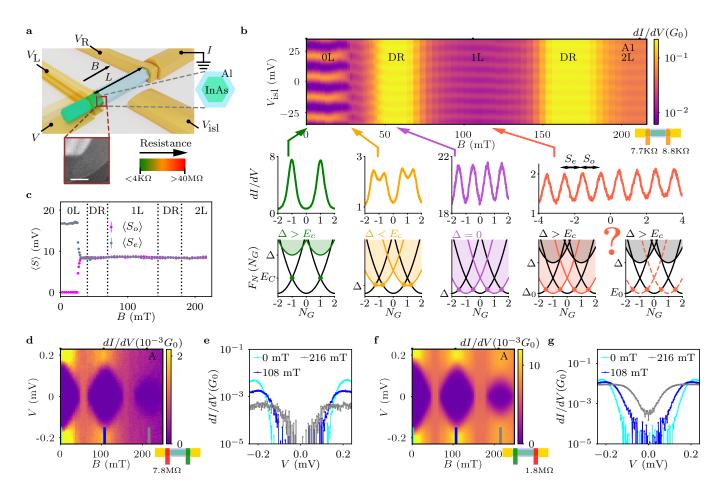


Figure 1: Experimental protocol for combining tunneling and Coulomb spectroscopy on the same device. (a) Schematics of a full-shell NW device. Turquoise represents the hexagonal InAs core, light blue the Al full-shell and gold the Ti/Au leads and gates. The AlOx layer separating the top gates and the tunnel junctions is not depicted. The insets show the NW cross-section schematic (right) and atomic resolution HAADF STEM image (left). The white scale bar corresponds to 20nm. (b) Zero-bias conductance dI/dV plotted in logarithmic scale, in units of $G_0 = 2e^2/h$, as a function of $V_{\rm isl}$ and magnetic field B for device A ($L \approx 700$ nm) with the tunnel barriers tuned to the intermediate-coupling regime. The ticks positioned on the upper axis of the figures correspond to integer multiples of the flux quantum Φ_0 . The NW free energy spectrum (see Eq. 1) and zero bias conductance versus normalized gate voltage N_G are shown below for B = 0 mT (green), B = 27 mT (orange), B = 56 mT (violet) and B = 116 mT (red). The conductance ranges are given in units of $10^{-2}G_0$. The 2-e to 1-e transport transition occurs within the Little-Parks zeroth lobe (0L) and 1-e-periodic spacing remains for the destructive regimes (DRs) and higher-order lobes (1L, 2L). (c) Coulomb peak spacing, $\langle S_e \rangle$ and $\langle S_o \rangle$, extracted from b. (d) [(f)] dI/dV as a function of V and B in the configuration where the left [right] junction is tuned to the weak coupling regime and the right [left] to the open regime. No signatures of sub-gap states are observed. (e) [(g)] Line-traces taken from (d) [(f)] at the center of the 0L (light blue), 1L (dark blue) and 2L (gray), showing a hard gap in the 0L and no ZBPs in the 1L.

robust against electrostatic tuning [31, 32, 33] and is ubiquitous for various material platforms [34, 35, 36, 37].

3 Experimental Protocol

In this work we devise a method based on the tuning of junction barriers that allows to compare the results of both spectroscopy techniques by applying them to the same device. Full-shell NWs, i.e., wires covered all around by the parent superconductor, are ideal for this purpose because MZMs are predicted to appear at well defined magnetic fields [12, 38]. In addition, the superconducting full-shell largely screens the electrochemical potential of the semiconductor core from external electric fields, so that the influence of junction tuning on a potential topological phase is minimized. The scheme of our devices is depicted in Fig 1a. We use full-shell Al/InAs NWs [39] and NWs for which the Al shell has been partially etched away (dubbed partial shell devices), in order to demonstrate the breadth of our results. The atomic resolution aberration corrected (AC) high angle annular dark field (HAADF) scanning transmission electron microscopy (STEM) images indicate a perfect epitaxy of the corresponding crystal lattices (see inset of Fig 1a and Fig S1 in the supplementary information (SI)). A hybridized semiconductor-superconductor island of length L is formed (see methods for fabrication details) and the transparencies of left and right junctions, consisting of bare InAs NW segments, are independently controlled by applying voltages V_L and V_R to the corresponding gates. The charge occupancy of the island is varied through the island gate voltage $V_{\rm isl}$. The gate configuration allows an in-situ tuning of the barrier transparencies, which in turn control the Coulomb charging energy $E_C = \frac{e^2}{2C_{\rm tot}}$ (where $C_{\rm tot}$ is the total capacitance of the island) [40]. For sufficient negative gate voltages it is possible to deplete the bare InAs junction and therefore switch off the devices from the left and right side independently. The transparency of the left (right) junction is characterized by the device resistance when the right (left) junction is completely on (see section 2 in the SI).

We distinguish between the island regime and the open regime. The latter has at least one very transparent barrier (colored in green) and a conductance measurement versus bias voltage V and $V_{\rm isl}$ does not reveal any E_C . For the island regime, we differentiate between the weak coupling regime (barriers colored in red) and the intermediate-coupling regime (barriers colored in orange). In the weak tunneling regime the subgap conductance at zero field is below the experimental noise level, while in the intermediate

spectroscopy regime increased subgap conductance is measured due to Andreev tunneling [41].

Here we report the findings for 7 full-shell islands ranging from 200 nm to 1 μ m, which we refer to as A ($L\approx 700$ nm), B ($L\approx 400$ nm), C ($L\approx 900$ nm), D ($L\approx 200$ nm), E ($L\approx 600$ nm), F ($L\approx 950$ nm) and G ($L\approx 1\mu$ m) and 2 partial shell islands which we refer to as pA ($L\approx 600$ nm) and pB ($L\approx 550$ nm).

We first focus on the Coulomb spectroscopy of device A (700 nm), see Fig. 1b. We investigate the Coulomb peaks in zero-bias differential conductance as a function of island gate $V_{\rm isl}$ and parallel magnetic field B. The magnetic flux along the superconducting shell gives rise to the Little-Parks (LP) effect, whereby the superconducting gap $\Delta(B)$ is periodically modulated by the flux Φ penetrating the NW cross section [42, 43]. The magnetic field intervals for which $\Delta \neq 0$, called as zeroth (0L), first (1L) and second lobe (2L), alternate with intervals where $\Delta = 0$, dubbed as destructive regimes (DRs). Each n = 0, 1, 2... lobe is associated with a number n of twists (or fluxoid number) of the superconducting phase around the shell, that grows by one each time the magnetic flux increases by a flux quantum $\Phi_0 = h/2e$.

To qualitatively understand the Coulomb blockade spectroscopy, we invoke the phenomenological energetic model [44, 45]. In thermodynamic equilibrium, the Gibbs free energy of an island with charge occupancy N and dimensionless gate-induced charge $N_G = \eta V_{\rm isl}/E_C$, is given by:

$$F_N(N_G, B) = E_C(N - N_G)^2 + \Delta(B)N \mod 2,$$
 (1)

where η is the lever arm. We perform the Coulomb spectroscopy measurement in the regime where $E_C < \Delta(B =$ 0). For each N, odd or even, F_N has a parabolic shape when changing N_G and the degeneracy points between two parabolas lead to Coulomb peaks in zero-bias conductance (marked as filled circles in the bottom insets of Fig. 1b). For zero magnetic field, Andreev processes give rise to coherent 2-e transport at these free energy degeneracy points as one electron drags a second one to create a Cooper pair [46] (green inset in Fig. 1b). Upon increasing the field, $\Delta(B)$ decreases and eventually vanishes, bringing the odd charge occupancy parabolas to zero energy. The 2-e peaks split at B = 27 mT (orange inset in Fig. 1b) as soon as $E_C > \Delta(B)$. When $\Delta(B) = 0$ (DR), the island exhibits 1-e periodicity signaling metallic single electron transport (violet inset in Fig. 1b).

As we increase the field further, the superconducting LP gap reopens and the condition $E_C < \Delta(B)$ for 2-e transport should be restored. However, instead of 2-e, we observe 1-e periodic transport (red inset in Fig. 1b), similar to the DR

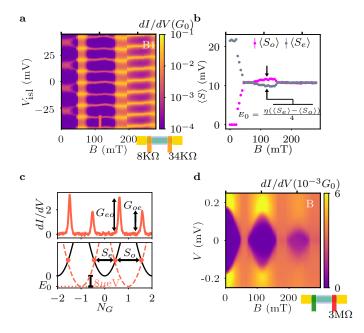
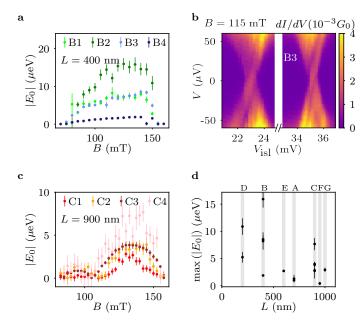


Figure 2: Coulomb and tunneling spectroscopy for a device with even-odd modulation. (a) Zero bias dI/dV as a function of $V_{\rm isl}$ and B in the intermediate-coupling regime. (b) Coulomb peak spacing, $\langle S_e \rangle$ and $\langle S_o \rangle$, extracted from a. (c) (top) Line-trace of a taken at $B=115{\rm mT}$ where the Coulomb peaks are not evenly spaced, i.e. $\langle S_e \rangle \neq \langle S_o \rangle$ (in units of $10^{-3}G_0$). Consecutive peak heights are denoted by G_{eo} and G_{oe} . (bottom) Energy of the system obtained from the panel above. The peak spacing in the upper panel corresponds to having a lowest energy state $E_0 \approx 8 \mu {\rm eV}$, see SI for details. (d) dI/dV as a function of V and B with V_R tuned in the weak tunneling regime and V_L tuned in the open regime, performing therefore tunneling spectroscopy from the right side.

transport. As a spectroscopic figure of merit, we compute the average spacing for odd and even Coulomb peaks, $\langle S_o \rangle$ and $\langle S_e \rangle$, corresponding to odd or even ground states, respectively. Fig. 1c depicts $\langle S_o \rangle$ and $\langle S_e \rangle$ as a function of B extracted from Fig. 1b. No measurable difference between $\langle S_o \rangle$ and $\langle S_e \rangle$ is observed in the DRs, in the 1L or in the 2L (Fig. 1c).

The 1-e transport could be explained either with a gapless superconducting island or with a subgap level of energy $E_0 \approx 0$, such as a MZM, see red inset of Fig. 1b. In order to clarify the validity of either of these scenarios we perform tunneling spectroscopy measurements at both ends of device A. It is important to note that there is one major difference between the two types of measurements. For Coulomb spectroscopy we need to form an island with E_C , while for tunneling spectroscopy we need to tune one of the junctions to the open regime in order to suppress E_C . In Fig. 1d we tune V_R to the open regime and V_L to the weak coupling regime and we investigate the evolution of dI/dV, as a function of B and V. Surprisingly, we cannot confirm at first sight either of the two possible scenarios. We observe no measurable conductance within a hard gap that follows the LP modulation, and no trace of a ZBP in the 1L consistent with an $E_0 \approx 0$ state that could support 1-e periodic transport in CB (Fig. 1e). We then reverse the voltages at the top gates, closing V_R and opening V_L and perform tunneling spectroscopy at the right side (see Fig. 1f). We again note the LP modulation and no subgap conductance above the noise level of our measurement or ZBP, as highlighted by the line-traces in Fig. 1g.

In order to understand whether the NW length has an effect on the above observations, we investigate device B which has a shorter length, $L \approx 400$ nm, and perform again tunneling and Coulomb spectroscopy. Figure 2a shows the Coulomb spectroscopy measurement with the tunnel barriers in the intermediate-coupling regime. Like in the previous device, the 0L is dominated by 2-e coherent transport. Again, in the 1L the 2-e coherent transport is not recovered. Unlike the previous case where Coulomb peaks where equally spaced in the 1L, see Fig. 1c, here the Coulomb peaks exhibit an even-odd pattern ($\langle S_e \rangle \neq \langle S_o \rangle$), see Figs. 2b and c. From $\langle S_e \rangle$ and $\langle S_o \rangle$ it is possible to extract the energy scale $E_0 = \eta\left(\frac{\langle S_e \rangle - \langle S_o \rangle}{4}\right)$. In the limit of low temperatures and contact transparencies, E_0 can be interpreted as the lowest electron-like subgap level (see SI for details) [47], although this connection should be expected to break down at higher transparencies, where higher-order transport processes dominate. At the middle of the 1L we can extract an energy of $E_0 \approx -8\mu \text{eV}$ (Fig. 2c bottom), i.e., very close to zero energy. Due to finite temperature in the experiment, a subgap level with such a small energy scale would lead to a broadened but visible ZBP in tunneling spectroscopy, since the $3.5k_BT$ Fermi broadening is about 15 μeV in our experiment (the effective electron temperature is about 50mK). However, the tunneling spectroscopy measurements in the weak tunneling regime from both island sides do not reveal any ZBP or other discrete subgap states in the first lobe (Fig. 2d and SI).



Tunability of even-odd modulation by Figure 3: junction gate voltages for different island lengths. (a) $|E_0|$ vs. B in the 1L for 4 different configurations of device B, which has a top gate and $L \approx 400$ nm. (b) dI/dVas a function of V and $V_{\rm isl}$ at B=115 mT, for configuration B3, demonstrating the presence of a ZBP and excited states. (c) $|E_0|$ vs. B in the 1L for 4 different configurations of device C, which has a side gate and $L \approx 900$ nm. (d) $\max\{|E_0|\}$ as a function of L. The grey columns include the different configurations of each device. It is clear that E_0 depends, at least equally important, on the junction transparencies as on the island length. It is important to notice that in previous works [13, 12], the reported value is $A = 4E_0$. For Majoranas E_0 should follow an exponentialdecaying law with L.

4 Controlling the even-odd asymmetry

To further investigate the nature of the even-odd modulation of the Coulomb peaks, we perform the same Coulomb spectroscopy experiment for different junction resistances of device B. In Fig. 3a we plot the absolute value of E_0 as a function of B taken in the 1L for four different junction configurations (B1, B2, B3 and B4; see Table ST3 for details about the junction resistances). Clearly, the voltages applied to the junctions strongly influence the E_0 modu-

lation, independently of island length L. For instance, at B=120 mT, E_0 can be tuned from above 15.4 μeV (configuration B2) to 1.6 μeV (configuration B4). Figure 3b furthermore demonstrates that transport takes place through a discrete resonance at low V, which is separated from a continuum at higher bias. However, we note that the observation or not of such a ZBP depends on the barrier configuration (see section 11 in the SI). In Fig. 3c we repeat the same analysis for device C, a long island device with $L\approx 900$ nm. Also for this device, it is possible to tune E_0 at B=140 mT from 7.3 μeV (configuration C4) to 2 μeV (configuration C1).

As a next step, we compare all the devices and all the configurations in terms of the maximum value of E_0 in the 1L. Fig. 3d shows $\max\{E_0\}$ as a function of L, with each grey column indicating the same device but different junction resistance configurations, see also Fig. S22. Once more, one observe that the junction resistances have an influence on E_0 comparable to the island length. A complementary figure of merit that could shed light on the potential presence of MZMs is the height difference between the odd Coulomb peak G_{eo} , and the even one G_{oe} , see top panel of Fig. 2c. Similarly, the peak height modulation strongly depends on junction properties (see SI).

5 Theory and discussion

In this final section we develop a theoretical picture, a variation of the gapless superconductor scenario, that resolves the apparent conflict between transport and CB spectroscopy. We focus on the following key experimental observations: (1) the dI/dV follows the LP effect but is otherwise rather featureless within the lobes; (2) the measured CB conductance peak spacing corresponds to a \sim 2e charging periodicity in most of the n=0 lobe, but is otherwise \sim 1e-periodic, with an even-odd modulation in n=1 corresponding to an $|E_0|\approx 0-20\mu {\rm eV}$ energy scale that depends strongly on sample and barrier configuration.

Our model of the islands follows closely the formalism of Ref. [12] (see Methods and SI). It allows us to simulate both the local density of states (LDOS) at any point of the island in a closed/closed barrier configuration (we choose a point inside the island adjacent to the left barrier), and also the dI/dV transport for closed/open islands. The results are summarized in Fig. 4. We first compute the subgap spectrum of a closed/closed $L=700 \mathrm{nm}$ -long island in a regime of high density and relatively small induced superconducting pairing on core states. We include spin-orbit coupling

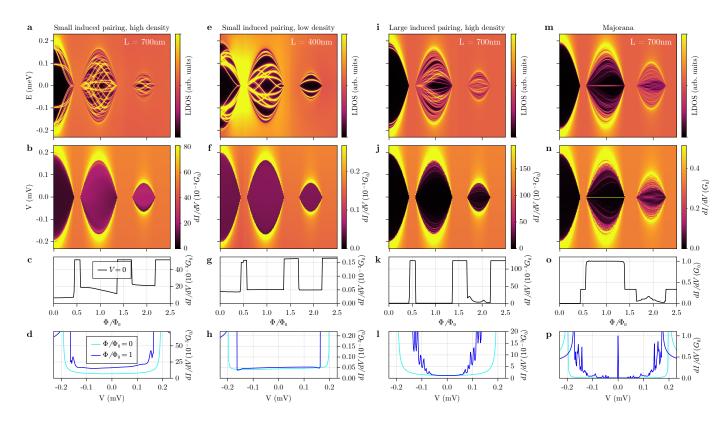


Figure 4: Numerical simulation of the single-particle local density of states (LDOS) and conductance (dI/dV) in full-shell nanowires. (a,e,i,m) LDOS in arbitrary units as a function of normalized flux Φ/Φ_0 and energy E for four different nanowire regimes: small induced pairing and high density, small induced pairing and density, large density and pairing and topological. The first two are the most representative of our experimental results. They differ only in the amount of charge transfer from shell to core and in the island length (see top-right corner), and exhibit a negligible and finite E_0 , respectively. The third, like the second, has a finite E_0 but is rather insensitive to barrier configuration. The topological case is carefully tuned to have two zero energy Majorana bound states within the first lobe (spatially localized at the barriers) by increasing the spin-orbit coupling sufficiently and tuning the chemical potential. All are weakly coupled to normal reservoirs across 100 nm long tunnel barriers at either end. The LDOS is taken at a nanowire section adjacent to the left barrier. In the limit of low temperatures and high barrier resistance, the subgap state of lowest energy E_0 controls the 1e period modulation in CB spectroscopy. (b,f,j,n) Tunneling dI/dV conductance as a function of bias V and flux in the same four systems, where the right-barrier is now fully open, deconfining subgap states into the right (normal) lead. The subgap features in the LDOS of the n=1 lobe become broadened. This is visible in conductance either as a smooth uniform background in the first two cases (strong broadening), or as weak and sharper U-shaped subgap features for large pairing, due to residual normal reflection at the right contact, (1). In contrast, a strong zero-bias anomaly due to the localized MBS on the left barrier remains clearly visible in the Majorana case (f). $(\mathbf{c},\mathbf{g},\mathbf{k},\mathbf{o})\ V=0$ cuts of the corresponding dI/dV. $(\mathbf{d},\mathbf{h},\mathbf{l},\mathbf{p})$ vertical cuts at $\Phi/\Phi_0=0,1$. All model parameters are given in Table ST14 of the SI.

(SOC), and choose a g-factor g=12. At zero magnetic field the longitudinally quantized normal-state levels inside the core are pushed away from zero energy due to the shell-induced pairing. However, a finite magnetic flux quickly breaks the induced pairing, which leads to a dense quasicontinuum of energy levels crossing zero in n>0 lobes, and even close to the edges of the n=0 lobe. This is consistent with the kind of unmodulated 1e-periodic CB phenomenology of device A, see 1(b,c), which would follow from the gapless metallic-like subgap quasicontinuum in the closed/closed small pairing regime (so $E_0=0$, understood as the energy of the lowest non-interacting excitation).

As the right barrier is opened to perform tunneling spectroscopy, the quasicontinuum of states is deconfined into the normal lead, smearing out the LDOS in the n>0 lobes into a weak uniform background inside the gap. Its uniformity is the result of strongly suppressed normal reflection at the right contact, made possible by the smallness of the pairing and the low normal resistance of the right barrier. The weak, uniform LDOS becomes visible in our simulations as a small but finite increase with n of the zero-temperature subgap dI/dV conductance background, see Fig. 4(b-d). Note that this increase was not detected in the dI/dV measurements of Figs. 1 and 2, an apparent conflict that will be addressed later on.

The regime of high density and small pairing above explains the CB spectroscopy of samples with $E_0 \approx 0$, like samples A or F. The emergence of a finite E_0 in other samples can be understood by considering a different regime with a shorter length L and/or a lower electronic density. In this case, the $n \neq 0$ subgap states acquire a larger level spacing, see Fig. 4e. The lowest of these longitudinally confined states has now a finite energy $E_0 \sim 1/L$, around $20\mu \text{eV}$ at its maximum in this instance. E_0 fluctuates strongly and stochastically with magnetic field and, notably, with barrier configuration, as the latter directly affects its longitudinal quantization condition, see Sec. 13.4 of the SI. Despite the complex LDOS dominated by mesoscopic fluctuations, and similar to the case of high density, opening the right barrier leads to a featureless dI/dV with no visible trace of E_0 , see Fig. 4(f-h). The increase in conductance background is much smaller in this case, but is still present. A third plausible scenario, also with a finite E_0 , is shown in Fig. 4(i-1). In this regime, both density and induced pairing are high, but E_0 exhibits a much smaller dependence of E_0 with barrier configuration, as it is dominated by the induced pairing, see SI. In summary, the range of behaviors of our model is consistent with the large variability of E_0 in our experiments. It also supports our observation that E_0 tends to decrease for longer islands, as also found in other experiments [12].

The above phenomenology is in stark contrast to the one expected in a topological island with Majorana bound states. The topological regime, as discussed in Ref. [12], is achieved by appropriate tuning of density and SOC. In Figs. 4(m-p) we have chosen a chemical potential in a topological phase and SOC has been artificially increased 25fold, as required to suppress the Majorana splitting across the L = 700nm island. The LDOS exhibits two Majorana bound states pinned to $E_0 = 0$. The left Majorana is localized close to the left barrier, so it is not significantly broadened upon opening the right barrier, unlike the right Majorana that readily delocalizes into the reservoir [48, 49]. The zero-temperature dI/dV shows a strong zero-bias anomaly, of universal height $G_0 = 2e^2/h$ in the limit of zero temperature and splitting, in contrast to the non-topological regimes in Figs. 4(b,f). Note, however, that at finite temperatures and deep in the tunneling regime, the G_0 peak height can be strongly reduced, so reducing tunnel resistance may be required to observe it [50].

The validity of our theoretical interpretation for the small or zero E_0 energy is contingent on the existence of a weak subgap background in the tunneling dI/dV that increases in $n \neq 0$ lobes relative to n = 0. This background increase stems from sequential tunneling through the LDOS quasicontinuum, that is ultimately responsible for the modulated 1-e periodicity of CB spectroscopy. (An *n*-independent cotuneling background is also expected for smaller L.) Our initial measurements failed to reveal this background increase. To verify the consistency of our interpretation we revisit the measurements of dI/dV versus V by increasing the resolution and decreasing the noise floor. As shown in Fig. 5(a,b), this allows us to detect a small but clear increase in subgap background conductance in the 1L as compared to the 0L (tunneling dI/dV in device B measured from left and the right contacts, respectively), as expected from our theory. The effect is also visible in the intermediate-coupling regime, see Figs. 5(c,d) and 4(b,c). Intermediate coupling softens the gap, but often also reveals subgap states similar to those in Fig. 4j, see SI. We note that the absence of a ZBP in the intermediate-coupling spectroscopy discards also the possibility that a MZM was not detected due to thermal broadening.

Finally, we investigate the generality of our findings by applying our experimental protocol to partial-shell NWs. Fig. 6a show the zero bias dI/dV as a function of $V_{\rm isl}$ and B for device pA (configuration pA1). As expected, the LP effect does not take place, and the superconducting gap gradually decreases till around 300 mT, where $\Delta=0$. The

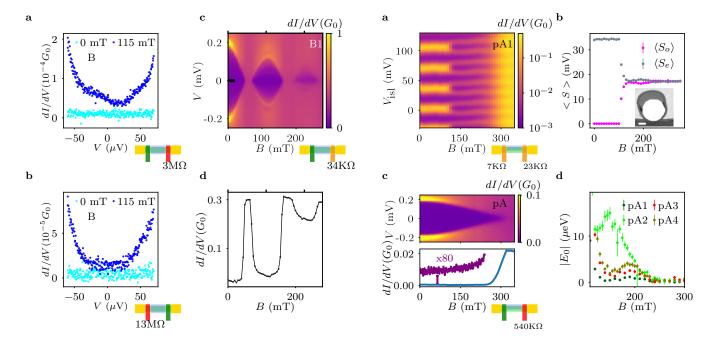


Figure 5: Conductance in LP lobes when increasing the measurement sensitivity or barrier transparency. (a) $[(\mathbf{b})]$ dI/dV of device B as a function of V taken in the middle of the 0L (dark blue) and the 1L (light blue) when performing the spectroscopy measurement from the left [right] side. It becomes obvious the subgap conductance in the 1L is enhanced. In order to resolve such low background conductance we decreased the noise floor at the expense of the total measurement time. (c) Intermediate-coupling spectroscopy performed from the right side. (d) Zero-bias conductance trace extracted from \mathbf{d} showing how the conductance increases within the LP lobes. dI/dV is plotted in logarithmic scale.

zero bias transport is 2-e periodic from 0 mT to 110 mT. At this point the 2-e Coulomb peaks split and develop an even-odd pattern, which becomes 1-e periodic at around 300 mT where superconductivity is completely destroyed. Fig. 6b depicts $\langle S_o \rangle$ and $\langle S_e \rangle$ as a function of B extracted from Fig. 6a. It is clear that $\langle S_e \rangle \neq \langle S_o \rangle$ from B=100 mT to B=230 mT, whereas for higher values of the field the transport becomes 1-e periodic. The extracted E_0 (see below) is below 7.5 μ eV and should be therefore observed as a ZBP. Similar to the full-shell devices, no ZBPs are observed in the tunneling spectroscopy measurement (see Fig. 6c). Similarly, no states appear in intermediate-coupling spectroscopy carried out with the same junction resistance as in

Figure 6: Behaviour of partial-shell devices. (a) Zero bias dI/dV as a function of $V_{\rm isl}$ and B for configuration pA1. (b) Plot showing the Coulomb peak spacing extracted from a. In the inset, a TEM image of a partial-shell device is shown. The white area is the InAs core and the Al, shown in grey, does not cover all the facets but only the upper part of the wire. The scale bar corresponds to 20nm. (c) (top) dI/dV as a function of V and B for device pA with one junction in the open regime and the other tuned in the weak coupling regime. The tunneling spectroscopy does not reveal a ZBP and/or subgap states. (bottom) Zero bias dI/dV vs B. The purple curve in the inset shows that the conductance background grows with B. (d) Plot showing E_0 vs. B for different configurations of the partial-shell device pA, i.e. pA1, pA2, PA3 and pA4.

Fig. 6a, see Fig. S16.

These observations support the previous findings from the full-shell devices that the the origin of the observed parity oscillations are not MZMs, but longitudinally-confined states brought down to low energies by the magnetic field through orbital effects. The orbital mechanism was also studied in Ref. [33] in the context of CB for partial-shell islands. For the sake of completeness, we studied the E_0 modulation for different barrier resistances also for the partial-shell devices. Fig. 6d shows E_0 as a function of B for 4 configurations of device pA. Again, E_0 can be dramatically

tuned by the junction resistances. Device pB, which shows similar behavior, is discussed in the SI (Fig. S36).

In summary, we have shown that 1-e Coulomb peak spacing results from a quasi-continuous subgap spectrum at finite field. Junction-dependent longitudinal confinement may lead to even-odd CB spacing modulation without visible low bias peaks in tunneling spectroscopy. Our work highlights the importance of junction details, even without quantum dot formation [20], for understanding transport spectroscopy in the quest for topological MZMs. Since topological edge states should theoretically be insensitive to such details, combined measurements on the same device like the ones presented here are an important step towards reducing ambiguities in interpretation. Length-dependence studies of MZM protection should take into account the possibility of junction-dependent longitudinally-confined modes as potential MZM false positives, and carefully discern algebraic (1/L) from exponential decays of even-odd modulations with length (see Fig. S42) [12, 13].

Methods

Fabrication

We use full-shell NWs which offer advantages in the search of MZMs, as they are predicted to appear at well defined magnetic fields [12, 38]. In addition, the superconducting full-shell largely screens the electrochemical potential of the semiconductor core from external electric fields. The hexagonal InAs NWs, with a diameter of about 110 nm, were grown via the vapor-liquid-solid (VLS) technique and the 30 nm Al shell was epitaxially grown in situ, giving a highly transparent semiconductor-SC interface [39]. The NWs were deposited on a heavily doped silicon substrate covered with 285 nm of silicon oxide. The superconducting island is formed by selectively etching Al from both sides of the NW (for the partial shell devices Al is also removed from some NW facets.) The bare InAs segments at the edges of the island are used as tunnel barriers. In all devices the tunnel junction length was chosen to be below 120 nm, in order to avoid a QD formation in the tunnel barrier regions [20]. The island gates and contacts consist of normal-metal (5 nm/180 nm Ti/Au bilayer). Two type of devices have been fabricated with top gates and with side gates. For the first type, a ≈ 9 nm thick layer of aluminium oxide is added at 150 °C by plasma atomic layer deposition, followed by deposition of normal-metal top gates (5 nm/180 nm Ti/Au bilayer). For the second type, the side gates are fabricated together with the ohmic contacts and the layout of the gates can be found in Fig.S27.

Device sampling/Short junction effect

Approximately 110 devices showed current at mK temperature when applying a voltage to the source and measuring a current through the drain. The tunnel junctions of the realized devices were purposefully fabricated in the short-junction limit in order to suppress QD formation [20] (see SI for device details). However, 18 of those showed ABS in at least one of the junctions and were therefore discarded. Furthermore, 78 did not show the required junction tunability, which we attribute to the short channel effect [51]. Finally 10 devices showed split Coulomb peaks and poisoning and were not further studied. The remaining 9 were fully characterized and are the focus of the present work.

Theory model

Full-shell nanowires were modeled as an axially symmetric, internal InAs semiconducting core of radius R = 60nm, covered by a 25nm-thick epitaxial Al superconducting shell. The electron subbands in the core are classified by their total angular momenta and remain decoupled in our model. The shell induces radial band bending and increased carrier density as one approaches the core/shell interface at r = R. Additionally, the shell induces superconducting correlations on core states by the proximity effect. The induced pairing Δ within lobe n acquires the same fluxoid number n of the parent Al order parameter, $\Delta \sim e^{in\phi}$. The absolute strength of the induced pairing depends on interface transparency, and is assumed here to be the most relevant difference between samples. The island is coupled to normal leads through ~ 100 nm-long potential barriers that can be tuned from tunneling to transparent regimes. This model allows us to simulate both the local density of states (LDOS) at any point of the island in a closed/closed barrier configuration, and also the dI/dV transport for closed/open islands. Both calculations are performed within a non-interacting electron approximation using the Quantica.jl package [52]. Further details on the model are provided in the SI.

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Author contribution. M.V., M.Bor. and G.K. designed the experiment. M.V. and M.Bor. fabricated the devices, performed the measurements and analyzed the data under the supervision of G.K.. A. H. and G. K. performed pre-characterization measurements on island devices. S.M.-S., M.Bot. and J.A. performed the HAADF STEM and EELS measurements. E.P., R.A. and P.S-J. provided theory support during and after the measurements, and developed the theoretical framework and models to analyze the experiment. E.P and P.S-J. performed the numerical simulations. M. V, M. Bor., E. P., R.A., P.S-J. and G.K. contributed to discussions and the preparation of the manuscript with input from the rest of authors.

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Data and Materials Availability: All experimental data included in this work and related to this work but not explicitly shown in the paper will be available via the IST Austria repository [https://doi.org/10.15479/AT:ISTA: 12102]. Code used for the data analysis, microscopy analysis data and the codes used for the numerical simulation can also be found at the IST Austria repository [https://doi.org/10.15479/AT:ISTA:12102].

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